NASA Contractor Report 4300

Modeling of Thermal Lensing in Side and End-Pumped Finite Solid-State Laser Rods

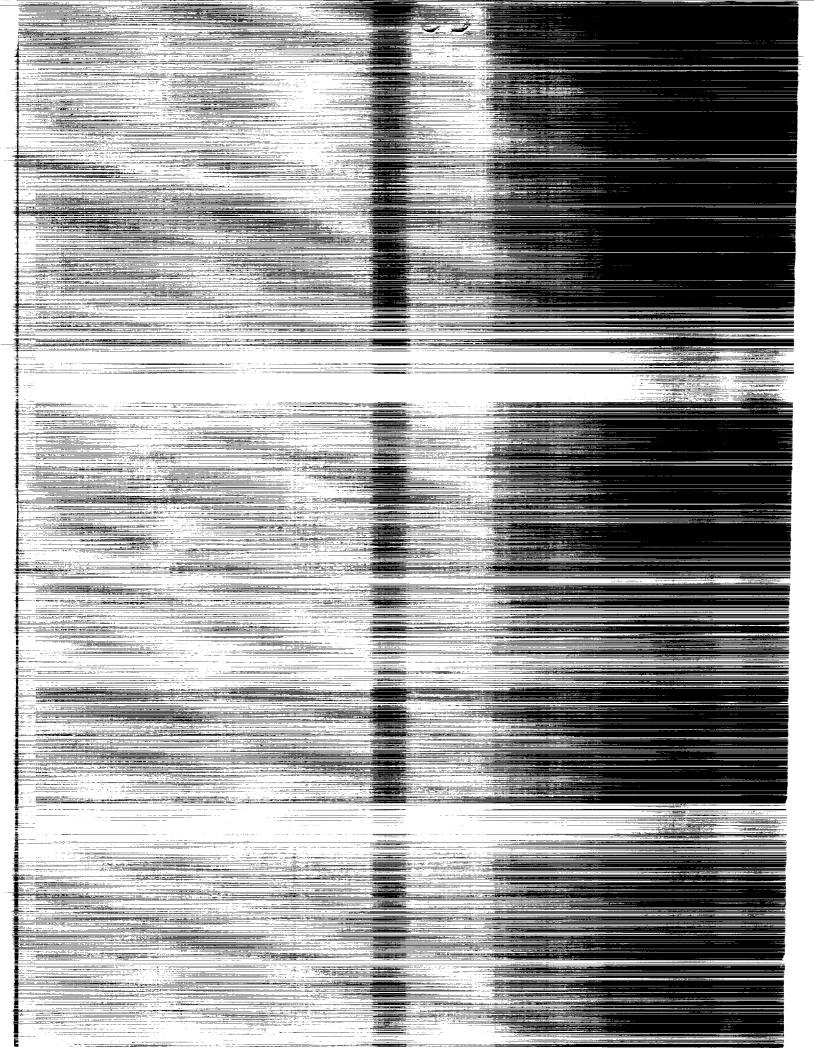
Vincent G. Brackett

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Modeling of Thermal Lensing in Side and End-Pumped Finite Solid-State Laser Rods

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Abstract

Modeling of Thermal Lensing in Side and End-Pumped Finite Solid-State Laser Rods

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An analytical expression for approximating the timedependent thermal focal length in finite solid-state laser rods has been derived. The analysis is based on the temperature variation of the material refractive index caused by optical pumping of these rods. Several quantities were found to be relevant to this analysis. These quantities were the specific thermal profiles of the rods, type of optical pumping employed, type of cooling scheme employed (side and end-cooling parameters), and the specific material characteristics of the rods. The Thermal Lensing Model was formulated using the geometric ray tracing approach. The focal lengths are then approximated, by calculating the phase shift in the index of refraction, as the different rays of an incident plane wave are tracked through a lenslike crystal medium. The approach also applies in the case of Gaussian or parabolic pump beams. It is shown that the prediction of thermal focal length is in good quantitative agreement with experimentally obtained data.

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CHAPTER 1

Introduction

The next generation of solid-state lasers (to be used for remote sensing of the atmosphere from space platforms), are under development. Various new lasing materials and laser configuations are being investigated. Currently, the solid-state, end-pumped diode lasers are the most promising candidates due to their small size, reliability, performance, low power and cooling requirements, etc. Analyzing thermal lensing effects for these end-pumped configuations, using various cooling schemes are of interest to the designers of laser systems. Theoretical formulation, numerical calculations, and experimental data on thermal lensing does not exist for end-pumped configuations.

The management of thermal energy deposited in a solidstate material is critical in the design of laser systems.
Any solid laser material operating in either pulsed or continuous wave (CW) mode of operation dissipates an appreciable amount of heat. The heat arises from non-radiative
energy transitions as the pump beam traverses the material.
Stated very briefly, when a material is excited to provide
more atoms (or molecules) in a higher energy state than in
some lower state, the material will be capable of amplifying radiation at the frequency corresponding to the ener-

gy level difference.² The acronym LASER derives its name from this process: "Light Amplification by Stimulated Emission of Radiation."

It's during this process that some fraction of the total energy of the pump beam is absorbed by the lasing mate-This absorbed energy is then dissipated as heat. the cylindrical geometries normally used, the heat is extracted from the surface of the cylinder, thereby generating a radial thermal gradient. Both radial and axial gradients are present in end-pumped lasers. Employment of active cooling to dissipate heat from laser crystals will also affect the thermal gradients. Therefore, the thermal gradients present in laser rods are governed by many fac-These include: geometries of the rod in use, type of laser material, thermal diffusivity of the material, and type of pumping and active cooling schemes employed. A Temperature Distribution Model has been developed to model the time dependent temperature distributions of finite solid-state laser rods that include the above factors. 1,3

The change in temperature, within a laser rod, causes thermal defocusing and distortion of the laser beam. This is due to the temperature variation of the material refractive index. These thermal gradients cause stresses within the laser material. The generated stresses induce birefringence and non-uniform expansion (bulge) in the laser

rod. Collectively, the above factors of temperature variation of the refractive index, induced birefringence, and bulge are called thermal lensing. Thermal lensing is the defocusing and distortion of a laser beam transmitted through a material medium, due to the non-uniform heating of the material.⁴

In this thesis, using the Temperature Distribution Model, thermal lensing effects will be analyzed to develop a Thermal Lensing Model. The Thermal Lensing Model will be employed to predict changes in the focal length and resultant distortions due to the time dependent temperature variations of the refractive index for two common laser materials that are under evaluation. These materials are Neodymium doped Yttrium Aluminum Garnet (YAG) (Y3AL5012) and Titanium doped Aluminum Oxide (Sapphire) (AL2O3). From this point onward, these two materials will be called Nd:YAG and Ti:AL2O3 respectively. They will be evaluated for various pumping (side and end) and cooling schemes. The induced birefringence and bulge caused by stress in the laser material will be discussed. However, these factors will not be implemented in the first version of the Thermal Lensing Model as they are minor in nature.

In the next chapter, the Temperature Distribution Model will be discussed. It's from this model's output that the time dependent temperature profiles are derived. These profiles serve as input to the Thermal Lensing Model.

CHAPTER 2

Temperature Distribution Model

The problem of managing the thermal energy deposited within a solid-state laser material under active pumping has long been of critical importance in the design of laser systems. 1 Koechner's paper on the transient temperature profile in solid-state lasers was the original work in this area. 5 In it, the time dependent temperature distribution of an infinitely long laser rod with a uniform heat source was determined. This configuation was adequate to treat the flashlamp pumping of relatively long laser rods, and rods with little or no end cooling employed. However, this treatment has become inapplicable to other pump configuations. Recently, several new solid-state laser materials have been introduced, each with their own thermal deposition mechanisms. 6 Additionally, several other novel laser techniques such as end-pumping with laser diodes have also been developed. For these systems, the assumptions of a uniform distribution of pump energy and an infinite rod length are no longer valid. The one dimensional approach of Koechner 5 does not apply when the length of the laser rod is comparable to its diameter. Furthermore, the longitudinal symmetry of an infinite rod is broken when it is end-pumped.

It was for these reasons that the Temperature Distribution Model was developed. The time dependent temperature distribution of a cylindrical rod of finite length has been derived by Farrukh et al. in two separate papers. 1,3 Additionally, they studied the evolution of thermal profiles for various pumping and cooling schemes. The general expression of the temperature distribution is given as:7

$$T(r,z) = \sum_{n,m=1}^{\infty} C_{nm} \phi_n(r) \ \psi_m(z) * f(t)$$
 (2-1)

where ϕ_n is the radial eigenfunction, ψ_m is the axial eigenfunction, c_{nm} is the pump pulse expansion coefficient, and f(t) is the time dependence function. The time dependence function f(t) for the on and off periods of the pumping pulse is given, respectively as:⁷

$$f(t) = \frac{\tau_{nm}}{\kappa * Lamda} * \begin{cases} \frac{\left(1 - e^{-\frac{n \text{cycle}}{\tau_{nm}}}\right)}{\left(1 - e^{\frac{\text{cycle}}{\tau_{nm}}}\right)} * \left(e^{-\frac{t - n \text{cycle} + \text{offtime}}{\tau_{nm}}}\right) \\ + \left(1 - e^{\frac{t - n \text{cycle}}{\tau_{nm}}}\right) \end{cases}$$
(2-2)

$$f(t) = \frac{\tau_{nm}}{K * Lamda} * \left\{ \frac{\left(\frac{1 - e^{-\frac{ncycle}{\tau_{nm}}}}{1 - e^{\frac{cycle}{\tau_{nm}}}}\right)}{\left(\frac{cycle}{1 - e^{\frac{cycle}{\tau_{nm}}}}\right)} * \left(e^{-\frac{t-ncycle + offtime}{\tau_{nm}}}\right) \right\}$$
 (2-3)

where K is the inverse of diffusivity, Lamda is the thermal conductivity, and τ_{nm} is the time constant for specific eigenfunctions.

The expression for temperature distribution is general and applies to various situations such as pulsed or continuous operations of the laser. A variety of different pumping and cooling schemes including end-pumping by a Gaussian beam were also discussed. To gain an appreciation for the capability of this model, we will look at two of the more interesting cases that this model can be used to evaluate. These are end-pumped single and multiple pulse operations for two common solid-state laser materials (Nd:YAG and Ti:AL2O3).

A. Single Pulse Operations

If a laser rod is pumped by a single pump pulse, a transient thermal profile will be established. This is the result of a fast pump-introduced heating process followed by a slow recovery of the rod to its ambient temperature. Although this thesis will primarily address long pump pulses, it is appropriate to distinguish the difference between short and long pump pulses. If the duration of the pumping pulse is very short in comparison to the laser rod relaxation time, then the heat energy deposited in the rod is considered to be deposited instantaneously. (The laser rod relaxation time is defined as the time required for the

rod to relax to its ambient temperature.) Rod relaxation times are approximately 3.5 seconds for Nd:YAG and 300ms for Ti:AL2O3 for typical rod dimensions. When a pulse is characterized as short or long, this characterization depends on the laser rod material. If the pump pulse duration is less than one percent of the relaxation time of the rod, then the pump pulse is considered to be short. In this case, as previously stated, the heat energy is deposited instantaneously. An example of this will be shown in a later graph. For long pulse operations, the heat energy being deposited builds up and relaxes simultaneously during the pumping pulse.

Figure 2-1 is an illustration of the transient nature of temperature distribution in an optically pumped cylindrical laser rod for a long pumping pulse. During the

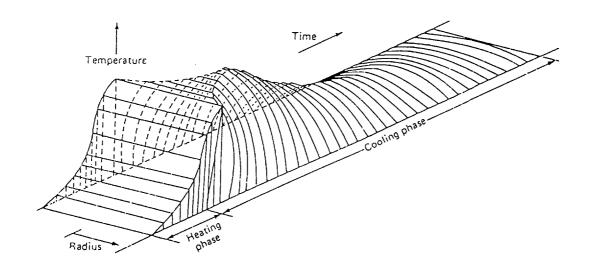
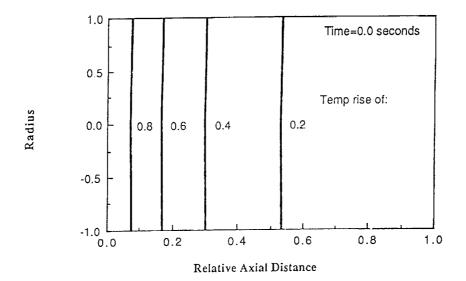


Figure 2-1. Thermal Relaxation of a Single Input
Pulse in a Cylindrical Laser Rod²

pulse, heat energy is absorbed by the laser crystal. At the end of the pump pulse, the temperature of the rod has increased above the ambient in a spatially non-uniform manner. Since only the surface of the rod is in contact with the coolant, a radial and axial heat flow develops during and at the end of the pump pulse. The initial non-uniform spatial temperature distribution changes to a nearly parabolic temperature profile which then decays at a rate determined by the rod specific relaxation time constant. Since lasing action occurs during or at the end of the pump pulse, the optical distortion in single pulsed lasers arises from the thermal gradients established during the pumped cycle.

Figure 2-2 and 2-3 are examples of the Temperature Distribution Model output for the time dependent heat propagation in end-pumped Nd:YAG and Ti:AL2O3 laser rods for a pump beam with spatially circular and Gaussian profiles respectively, with moderate side cooling. In both of these figures, the energy absorbed as heat, is 1J/cm³ at the front end of the rod for the circular pump and at the center of the front end for the Gaussian pump. Figure 2-2 was chosen as an example because it shows the impact of side cooling in generating radial gradients in a Nd:YAG rod after only 20ms into its thermal relaxation cycle. Also in Figure 2-2, the temperature at the center of rod has not



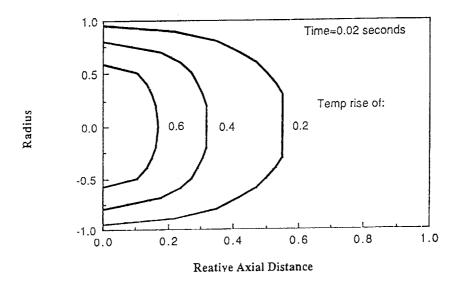
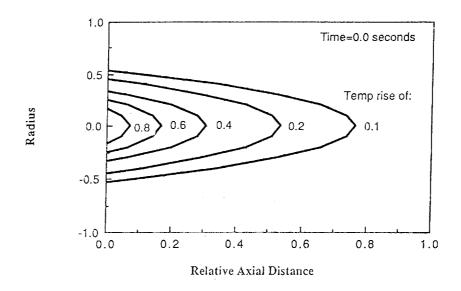


Figure 2-2. <u>Heat Propagation in Nd:YAG Laser Rod</u>
(End-Pumped, Single Pulse with a
Uniform Cross Section Pumping Beam)



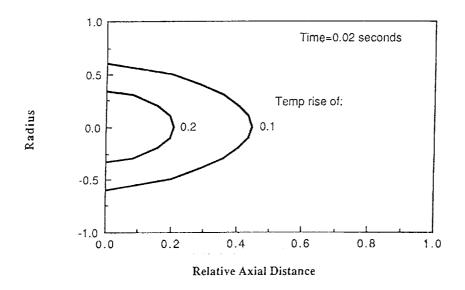


Figure 2-3. Heat Propagation in Ti:AL2O3 Laser Rod (End-Pumped, Single Pulse with a Gaussian Cross Section Pumping Beam)

appreciably relaxed toward the ambient temperature at the 20ms point in time. Figure 2-3 was chosen as an example to illustrate the difference between a circular and Gaussian pumping beam. This figure also shows that after only 20ms into the thermal relaxation cycle, the Ti:AL2O3 laser rod has significantly relaxed toward its ambient temperature. However, the thermal energy content in the Gaussian pump case is only about 1/8 of that of the circular pump case.

Figure 2-4 is an example of the model output of the temperature rise above ambient for five different pulse durations for a Nd:YAG laser rod with one pulse of 50mJ of absorbed energy. The Nd:YAG laser was end-pumped with a Gaussian beam and subjected to moderate side cooling. The rod ends were not cooled. The lms pulse in this figure is an example of a short pulse where the heat energy is deposited instantaneously. The remaining pulses in this figure are examples of relatively long pulses. In Figure 2-4, the rod has essentially relaxed to the ambient temperature approximately 3.5 seconds after completion of the pumping pulse.

Figure 2-5 is an example of the model output of the temperature rise above ambient for five different pulse durations for a ${\tt Ti:AL_2O_3}$ laser rod using 50mJ of absorbed energy per pulse. The ${\tt Ti:AL_2O_3}$ laser rod was end-pumped with a Gaussian beam and subjected to moderate side-

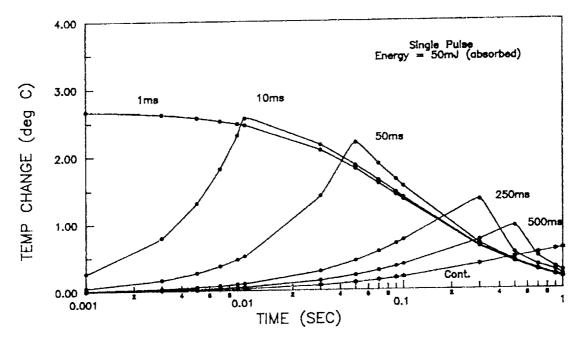


Figure 2-4. Temperature Profiles for Various

Durations of a Single Pump Pulse for

Nd:YAG (At Center of Pump-End Face)

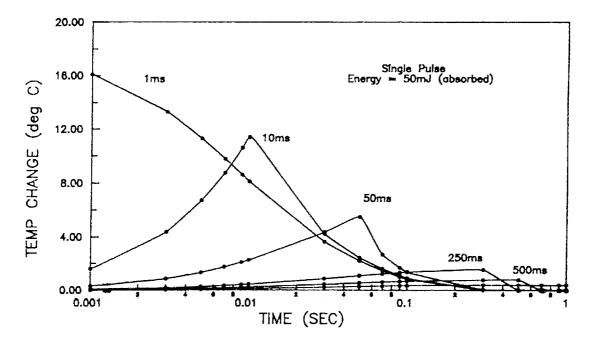


Figure 2-5. Temperature Profiles for Various

Durations of a Single Pump Pulse for

Ti:AL₂O₃ (At Center of Pump-End Face)

cooling. The rod ends were not cooled. The lms pulse in this figure is an example of a short pulse where the heat energy is deposited instantaneously. The remaining pulses in this figure are examples of relatively long pulses. In Figure 2-5, the rod has essentially relaxed to thermal equilibrium approximately 300ms after completion of the pumping pulse.

Comparison of Figures 2-4 and 2-5 also shows that the Ti:AL₂O₃ rod has a greater temperature rise than the Nd:YAG rod under the same conditions of absorbed energy, pulse duration, and cooling scheme. These results are not unexpected as the thermal conductivity of Ti:AL₂O₃ is higher than Nd:YAG.

B. Multiple Pulse Operations

In the previous section, we discussed pump induced thermal profiles that occur for single-pulse operations. The pulse input intervals are long with respect to the thermal relaxation times of the laser rod. Additionally, the rod has returned to the ambient temperature before the onset of the next pumping pulse. If the laser is operated at a repetition rate at which there exists a residual temperature distribution from the previous pulse, a temperature buildup in the rod will occur. The temperature at specific points will increase until a steady-state condition is reached. Figure 2-6 is an illustration of the tem-

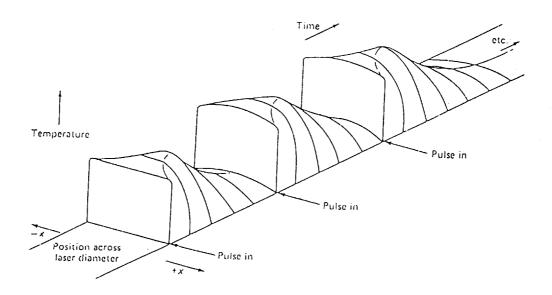


Figure 2-6. Thermal Relaxation in a Solid Cylinder with Pulse Input Intervals near the Thermal Relaxation Times 2

perature profile of a laser operated at a low repetition rate.

Figure 2-7 is an illustration of thermal buildup at a pulse interval smaller than the thermal relaxation time. Under these conditions, the laser will soon establish a steady-state operating condition where the radial and axial rate of flow of heat out of the rod will equal the rate of heat deposition. During the transition period, the rod radial and axial thermal profiles will continue to change until the steady-state equilibrium temperature is reached. In the extreme case, when the interval between pulses be-

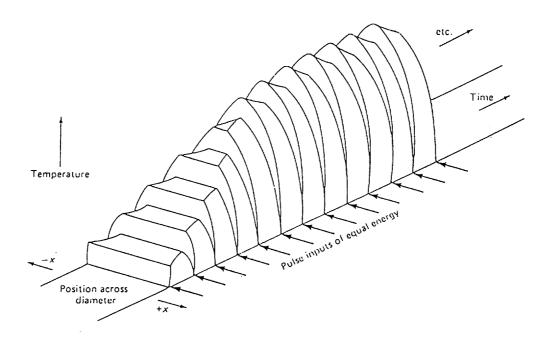


Figure 2-7. Thermal Buildup when Pulse Interval is Small Compared to Thermal Relaxation Time²

comes negligibly small compared to the thermal relaxation time, the thermal profile of the laser rod will approach the profiles of continuously pumped rods with the same total power deposition. The transient temperature distributions, as the rod approaches thermal equilibrium, has a large effect on the laser energy output and beam divergence of the laser². These transient periods will be discussed in the next chapter on thermal lensing.

Figures 2-8 and 2-9 are examples of a Gaussian endpumped Nd:YAG laser being operated at a high pulse repetition rate. Figure 2-8 depicts the detailed buildup of tem-

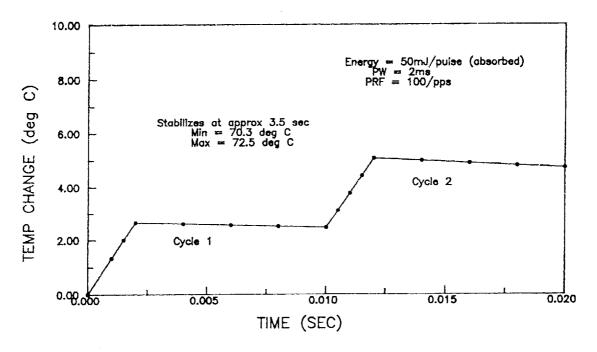


Figure 2-8. <u>Variation of Temperature for Nd:YAG</u>
(At Center of Pump-End Face)

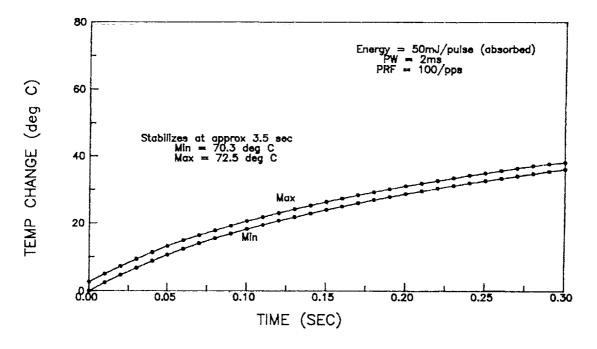


Figure 2-9. Extreme Temperature for Nd:YAG
(At Center of Pump-End Face)

perature for two pump cycles. Figure 2-9 shows the maximum and minimum temperatures within each pulse cycle. These graphs show that the Nd:YAG laser will reach a steady-state temperature in approximately 3.0 seconds. The estimated maximum temperature of the Nd:YAG rod is approximately 72.5°C above the ambient at the center of the rod pump-end face.

This knowledge of the maximum temperature is critical to laser design. For example, if the temperature exceeds the stress fracture limit of the rod, the laser crystal will fracture. The stress fracture temperature limit for Nd:YAG is approximately 115°C.²

Figure 2-10 and 2-11 are examples of the output from

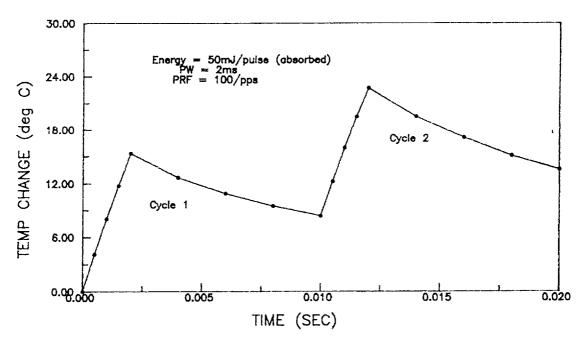


Figure 2-10. <u>Variation of Temperature for Ti:AL₂O₃</u>
(At <u>Center of Pump-End Face</u>)

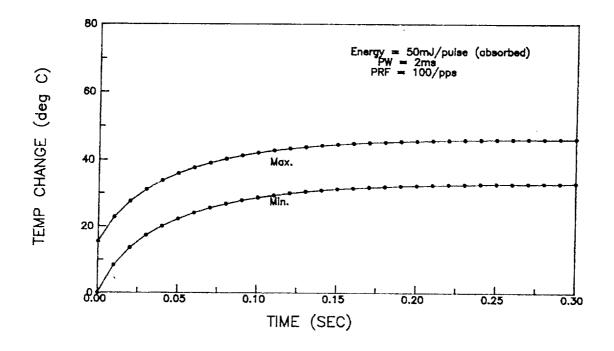


Figure 2-11. Extreme Temperature for Ti:AL₂O₃
(At Center of Pump-End Face)

the Temperature Distribution Model of the temperature rise due to accumulation effects of multipulse operations for Gaussian end-pumped Ti:AL₂O₃ rods. As can be seen, the rod reaches a steady-state temperature in approximately 300ms and has a maximum temperature of approximately 42°C at the center of the pump-end face.

The above presented example profiles from the Temperature Distribution Model are just a few of the many profiles that can be generated. Other profiles, such as radial and axial temperature profiles versus time, can also be generated for a variety of pumping and cooling schemes.

C. Summary of the Temperature Distribution Model

The general theory describing the transient thermal profiles in CW and pulse-pumped lasers for a large variety of operating parameters are presented in Koechner^{2,5} and Farrukh et al.^{1,3,7} These general theories were implemented by Farrukh into a general analytical model. The model then generates thermal profiles for a large variety of finite solid-state lasers, with user specified operating parameters. Examples of typical profiles were presented throughout this section to give the reader a feel for the capabilities of this model.

These time-dependent derived thermal profiles are critical in determining thermal lensing effects which depend upon the spatial distribution of temperature and its gradients.

In the next chapter, the theory of thermal lensing and formulation of the Thermal Lensing Model will be discussed. The model takes as its input, the time-dependent temperature profiles from the Temperature Distribution Model outlined above. The Thermal Lensing Model is then used to estimate the focal lengths and distortions present in finite solid-state Nd:YAG and Ti:AL2O3 laser rods.

CHAPTER 3

Thermal Lensing

A. Introduction to Thermal Lensing.

Thermal lensing is the distortion and defocusing of a laser beam transmitted through material medium, due to the non-uniform heating of the material.⁴ Any solid-state laser material operating in either the steady-state, pulsed, or CW mode of operation must dissipate an appreciable amount of heat. This is the result of a fast pump-introduced heating process (where some fraction of the total pump energy is deposited in the laser rod as heat), followed by a slow recovery of the rod to its ambient temperature. In the cylindrical rod geometries normally used, the heat is removed on the surface of the rod. This process generates radial and axial thermal gradients in the rod.

The change in temperature, within a laser rod, causes thermal defocusing and distortion of the laser beam. This is due to the temperature variation of the material refractive index. Additionally, these thermal gradients cause stresses within the laser material. The generated stresses induce birefringence and non-uniform elongation of the rod and bulging of the ends. Collectively, these above factors of temperature variation of the refractive index, birefringence, and bulge are referred to as thermal lensing. From

Koechner⁹, the temperature dependent variation of the refractive index constitutes the major contribution to thermal lensing. The stress dependent variation of the refractive index (birefringence) modifies the focal length about 20 percent.⁹ The effects of end-face curvature, caused by an elongation of the rod on thermal lensing is less than six percent.⁹

The resulting distortion and defocusing of laser beams have been observed in a variety of experiments. Several theoretical treatments of thermal lensing have been given. These include geometrical-optics 10 , wave-optics 11 , and the vector Kirchhoff diffraction formulation of thermal lensing 4 , 11 to account for thermally-induced birefringence.

In the general theory for the formulation of the Thermal Lensing Model, various effects of thermal lensing will be discussed. However, in the model, only thermal lensing due to the temperature variation of the material refractive index using ray-trace methodology will be implemented. The ray-trace method was chosen as the simplest approach to obtain a working model. This method makes maximum use of the temperature profiles generated by the Temperature Distribution Model previously discussed. This approach also accounts for 75-80 percent of the thermal lensing effects present in side and end-pumped laser rods. In general, the model will give the user a first approximation of the

thermal focal length and the degree of distortion expected for rods of specific dimensions and specified operating parameters. The input to this approach will be the temperature profiles generated by the Temperature Distribution Model.

In the next section, a detailed one dimensional theory of thermal lensing from Koechner^{2,9} will be presented. The presented theory will outline the effects of temperature, birefringence, and bulge that contribute to thermal lensing for a side-pumped Nd:YAG laser rod.

B. One Dimensional Theory of Thermal Lensing.

The one dimensional theory of thermal lensing is looked at because the basic underlying theory and mathematical formulation can be modified and applied to the problem of developing the Thermal Lensing Model.

consider the case of the CW side-pumped Nd:YAG rod where the heat generated within the laser rod, due to the optical pumping, are removed by a coolant flowing along the cylindrical rod surface. As a result of the assumption of uniform internal heat generation and uniform cooling along the cylindrical surface of an infinitely long rod, the temperature profiles will be strictly radial. The end effects and small variation of coolant temperature in the axial direction are neglected here. The radial temperature distribution in a very long cylindrical rod is obtained from the

one dimensional heat conduction equation: 13

$$\frac{d^2T}{dr^2} + \frac{dT}{rdr} + \frac{Q}{K} = 0$$
 (3-1)

where K is the material thermal conductivity and Q is the rate at which heat is generated per unit volume. The solution to equation (3-1) gives the temperature at any point along a radius of length r. With the boundary condition $T(r_0)$ for $r=r_0$, where $T(r_0)$ is the temperature at the rod surface and r_0 is the radius of the rod, then:

$$T(r) = T(r_0) + \frac{Q}{4K}(r_0^2 - r^2)$$
 (3-2)

This temperature profile is parabolic, with the highest temperature being at the center of the rod. The heat generated per unit volume, for uniform heat absorbtion, can be expressed as:

$$Q = \frac{P_a}{\pi r_o^2 L}$$
 (3-3)

where P_a is the total power absorbed by the rod; r_o is the rod radius; and L is the length of the rod. The temperature difference between the rod surface and the center is given by:

$$T(0) - T(r_0) = \frac{P_a}{4\pi KL}$$
 (3-4)

The transfer of heat between the rod and the coolant

and the coolant. A steady-state equilibrium temperature will be reached when the rate of the total internal generation (Pa) of heat is equal to the rate at which heat is removed from the rod by the coolant. For a typical Nd:YAG rod, the equilibrium temperature is reached about 3 1/2 seconds after laser turn-on. Figure 3-1 depicts an example of the radial temperature profile of a 20 pulse per second, side-pumped, Nd:YAG laser at thermal equilibrium.

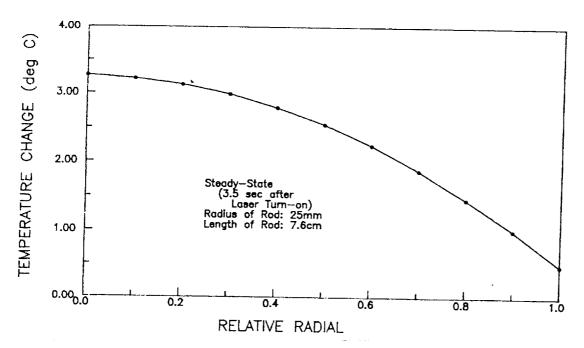


Figure 3-1. Radial Temperature Distribution for a Nd:YAG Crystal

The heat is generated at the rate of 0.3 Joules per pulse and negligible cooling was assumed at the ends of the rod. With these conditions, axial thermal gradients do not exist

in this rod.

These temperature gradients generate mechanical radial, tangential, and axial stresses in the laser rod, since the hotter inside area of the rod is constrained from expansion by the cooler rod surface. Normally, these stresses are calculated when one needs to find the birefringence and the stress fracture limit of the crystal. For Nd:YAG rods, Koechner^{2,9} has provided a sample of these calculations. For example, if the approximate temperature differential between the center and the surface of the rod is 115°C, then the crystal may fracture. The equations for these calculations are derived by Timoshenko and Goodier. 15

Having discussed the basic theory of one dimensional temperature distribution and the mechanical stresses caused by the thermal gradients, our attention can now be turned to the photoelastic effects (birefringence). The mechanical stresses generate thermal strains in the rod, which in turn produce refractive index variations via the photoelastic effect. The refractive index of a medium is specified by the indicatrix. In its most general case, the indicatrix is in the shape of an ellipsoid. A change of refractive index due to strain is given by a small change in the shape, size, and orientation of the indicatrix. 16 Since Nd:YAG is a cubic crystal, the indicatrix is a

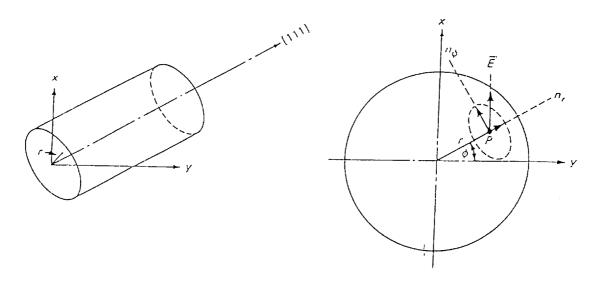


Figure 3-2. Crystal Orientation for a Nd:YAG Rod (left) and Orientation of Indicatrix of a Thermally Stressed Rod in a Plane Perpendicular to the Rod Axis (right)²

sphere. Under stress, the indicatrix becomes an ellipsoid. Nd:YAG rods are grown with the cylindrical axes along the [111] direction. An illustration of this is depicted in Figure 3-2. The light propagates in this direction, and thus the change of the refractive index along the [111] axis is of interest.

Since the transverse stresses are in the radial and tangential direction (see Figure 3-2), the local indicatrix also orients its axis in those directions. In a cylindrical coordinate system, the photoelastic changes in the refractive index for the radial and tangential polarizations are only obtained after a considerable amount of tensor

analysis. This is normally done using the vector Kirchhoff diffraction formulation approach. Various treatments of these involved birefringence calculations for Nd:YAG are covered in detail in references 4, 8, 12, and 17. The expressions for the radial and tangential refractive index changes for Nd:YAG are given by^{8,17} as:

$$\Delta n_r = -\frac{1}{2} n_o^3 \frac{\alpha Q}{K} C_r r^2 \tag{3-5}$$

$$\Delta n_{\phi} = -\frac{1}{2} n_o^3 \frac{\alpha Q}{K} C_{\phi} r^2 \tag{3-6}$$

where Δn_r and Δn_ϕ are the radial and tangential stress dependent changes of the refractive index, respectively; n_0 is the refractive index of the rod at its ambient temperature; α is the thermal coefficient of expansion for Nd:YAG; Q is the heat generated per unit volume; and K is the thermal conductivity of Nd:YAG. The coefficients C_r and C_ϕ are functions of the electrooptical coefficients that were determined from tensor analysis for Nd:YAG. Both coefficients were calculated by Koechner² for Nd:YAG. Their values are listed as $C_r = 0.017$ and $C_\phi = -0.0025$ respectively.

Having explored the temperature and stresses in a Nd:YAG rod, the optical distortions which are a result of both the thermal gradients and the stresses can now be discussed. The change in the refractive index can be separated into a temperature and a stress-dependent contribu-

tion.² Therefore:

$$n(r) = n_0 + \Delta n(r)_T + \Delta n(r)_S$$
 (3-7)

where n(r) is the radial variation of the refractive index; n_0 is the refractive index of the material at ambient temperature; $\Delta n(r)_T$ and $\Delta n(r)_S$ are the temperature and stress-dependent changes of the refractive index, respectively.

The temperature dependent change of the refractive index can be expressed as: 2

$$\Delta n(r)_{T} = [T(r) - T(0)] \frac{dn}{dT}$$
 (3-8)

where T(r) and T(0) are the temperature at the radius r and center of the rod, respectively. With the aid of equations (3-2 through 3-4) and equation (3-8), we obtain:

$$\Delta n(r)_{T} = -\frac{Q}{4K} \frac{dn}{dT} r^{2}$$
 (3-9)

Comparing equations (3-5, 3-6, and 3-9), we see that the refractive index in a laser rod shows a quadratic variation with radius. An optical beam propagating along the rod axis also develops a quadratic spatial phase variation. This perturbation is equivalent to the effect of a spherical lens¹⁴. The focal length of a lens-like medium whose index of refraction is assumed to vary according to:²

$$n(r) = n_0 \left(1 - \frac{2r^2}{b^2} \right)$$
 (3-10)

where b measures the degree of variation of the index of refraction is given by: 14

$$f = \frac{r^2}{4n_0L} \tag{3-11}$$

The total variation of the refractive index is obtained by introducing equations (3-5, 3-6, and 3-9) into (3-7). This gives us: ²

$$n(r) = n_o \left\{ 1 - \frac{Q}{2K} \left(\frac{1}{2n_o} \frac{dn}{dT} + n_o^2 \alpha C_{r,\phi} \right) r^2 \right\}$$
 (3-12)

As was previously discussed, the change in the refractive index, due to thermal strain, is dependent on the radial (r) and tangential (ϕ) stresses where C_r = 0.017 and C_{ϕ} = -0.0025. Therefore, the expression for n(r) in (3-12) yeilds two values. Comparing equations (3-10) and (3-12) yields the focal length (f') equation: ²

$$f' = \frac{K}{QL} \left(\frac{dn}{2dT} + \alpha C_{r,\phi} n_o^3 \right)^{-1}$$
 [3-13]

The first term in the parentheses is the temperature dependent variation of the refractive index. The second term contains the stress dependent variations of the refractive index. Because of the birefringence, Nd:YAG has two effective focal lengths. One is due to the radial electrooptic

 $(\mathtt{C}_{\mathtt{r}})$ coefficient and the second is due to the tangential (\mathtt{C}_{\emptyset}) coefficient.

In our final expression for the focal length of a Nd:YAG rod, we must also include the effect of rod end distortion (bulge). The stresses, that cause bulging, are found to occur within a region of approximately one radius from the ends for Nd:YAG. 18 This deviation from flatness of the rod ends is obtained from: 2

$$L(r) = \alpha L_0[T(r) - T(0)]$$
 (3-14)

where α is the thermal coefficient of expansion for Nd:YAG and L_0 is the length of the end section of the rod where expansion occurs. With L_0 = r_0 and equation (3-2), we obtain:²

$$L(r) = -\alpha r_0 \frac{Q r^2}{4K}$$
 (3-15)

The contribution to the focal length of the rod caused by end-face curvature is given by the thick-lens formula of geometric optics 16 as:

$$f'' = \frac{R}{2(n_p - 1)}$$
 (3-16)

where the radius of end-face curvature is defined as $R = -(d^2L/dr^2)^{-1}$. From the expressions (3-14, 3-15, and 3-16) follows the focal (f") length of the rod caused by bulge:²

$$f'' = K[\alpha Qr_o(n_o - 1)]^{-1}$$
 (3-17)

Inserting equation (3-17) into (3-13) gives us the final expression for the focal length of a Nd:YAG rod:²

$$f = \frac{KA}{P_a} \left(\frac{dn}{2dT} + \alpha C_{r,\phi} n_o^3 + \frac{\alpha r_o(n_o - 1)}{L} \right)^{-1}$$
 (3-18)

where A is the rod cross-sectional area and P_a is the power absorbed.

This expression accounts for the temperature, stress-dependent variation of the refractive index, and end-face curvature. If one introduces the appropriate material parameters for Nd:YAG into equation (3-18), then one finds that the temperature dependent variation of the refractive index constitutes the major contribution to thermal lensing.² The stress dependent variation of the refractive index and end-face curvature modifies the focal length by approximately 20 percent and less than 6 percent, respectively.²

Figure 3-3 depicts the graph of the approximation of the focal lengths, using equation (3-18), for a side-pumped Nd:YAG rod. The focal lengths were calculated using the following parameters: length and radius of the rod was 7.6cm and 25mm, respectively; dn/dt, the material variation of the refractive index was 8.9 x 10^{-6} ; index of refraction

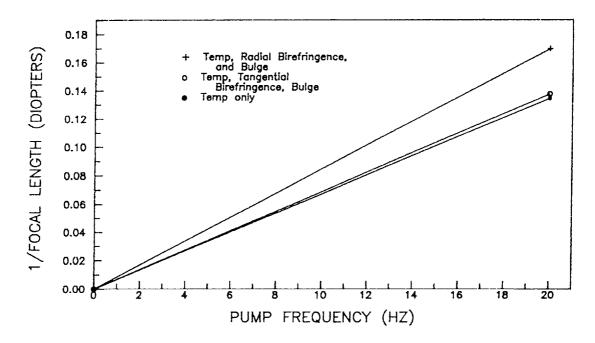


Figure 3-3. <u>Predicted Thermal Focusing Effects</u> in Nd:YAG

 (n_0) was 1.825; thermal conductivity (K) was 0.103; α , the thermal coefficient for expansion was 7.9 x 10^{-6} ; the radial (C_r) and tangential (C_{ϕ}) variation of the refractive index were 0.017 and -0.0025, respectively; and, the power absorbed (P_a) by the rod (as heat), was 6.119w/cm³.

This completes the one dimensional theory of thermal lensing for a Nd:YAG rod. The same analysis holds for Ti:AL2O3 and other laser materials. As was previously stated, the temperature dependent variation of the refractive index will be the only aspect implemented in the Thermal Lensing Model. The implementation of birefringence and bulge effects will be left as future enhancements to the

model. In the next section, the formulation of the Thermal Lensing Model is developed.

C. Two Dimensional Model Formulation.

requires basic understanding of various optical theories. These include the theories of ray tracing¹⁶, wave optics in crystals^{11,19}, Fresnel diffraction theory of waves in lenslike mediums¹⁴, geometrical-optics¹⁰, etc. It was not the purpose of this thesis to become trapped into the finer details of the referenced optic theories. Nor do we intend to repeat the derivations of the referenced theories. If more detailed information is desired, then we refer the reader to the attached list of references and other literature on the subject.

The basic task of this research is to formulate a computer ray-trace model that allows for a first approximation of focal length. The model is to be based on the temperature variation of the refractive index. The approximations of focal length are then obtained on specific crystals operated with specified parameters. This will be done by modifying the focal length expression (3-11) for a thin lens. The focal lengths are then approximated, by calculating the phase shift in the index of refraction, as the different rays of a plane wave front are tracked through a lens-like crystal medium. The localized change in the ray

direction as it transverses a lens-like medium is assumed to obey Snell's law which is given by: 19

$$n_1 \sin \theta_0 = n_2 \sin \theta_i \tag{3-19}$$

where n_1 and n_2 are the index of refractions of two adjacent mediums, respectively; and θ_i and θ_o are the input and output angles of the ray at the boundary between the adjacent mediums.

To assist in the formulation of the model, it is appropriate to introduce, and explain, two tables and a figure before proceeding. Table 3-1 depicts an illustration of the output block of radial and axial temperature profiles, provided by the Temperature Distribution Model.

This output is based on a 20pps, side-pumped, Nd:YAG laser.

The laser was operated with moderate side cooling and rod

Table 3-1. <u>Block of Radial and Axial Temperature</u>
Profiles for a Nd:YAG Crystal

Temperature Distribution Radial Diffusivity						
R\L	0.00		0.50		1.00	
0.00 0.20 0.40 0.60 0.80 1.00	2.9139 2.8020 2.4660 1.9047 1.1276 0.2248		2.9139 2.8020 2.4660 1.9047 1.1276 0.2248		2.9139 2.8020 2.4660 1.9047 1.1276 0.2248	

ends were not cooled. In the vertical direction, are the radial temperatures starting from the center of the rod (top) and increments outward to the surface of the rod (bottom). In the horizontal direction, are the axial temperatures starting from the front face (left) of the rod and increments to the back end (right) of the rod. In this particular example, a set of 10 equally spaced increments was chosen to represent the 25mm x 7.6cm rod in both the axial and radial directions. Additionally, in Table 3-1, the temperatures are observed only to vary in the radial direction. The displayed block of temperatures in Table 3-1 is an example of a side-pumped Nd:YAG rod at thermal equilibrium, when rod ends aren't cooled.

Table 3-2 displays a block of radial and axial index of refractions for the temperatures presented in Table 3-1.

Table 3-2. Block of Radial and Axial Index of Refraction for the Temperatures in Table 3-1

Index of Refractions								
R\L	0.00		0.50	• • •	1.00			
0.00 0.20 0.40 0.60 0.80 1.00	1.825026 1.825025 1.825022 1.825017 1.825010 1.825002		1.825026 1.825025 1.825022 1.825017 1.825010 1.825002		1.825026 1.825025 1.825022 1.825017 1.825010 1.825002			

The block of temperature variations of the Index of Refractions were calculated from the expression:

$$n(r,z) = n_0 + \alpha T(r,z)$$
 (3-20)

where n_0 is the index of refraction for the rod at its ambient temperature and α is the dn/dt specified for the rod.

Table 3-2, shows that the index of refraction is only changing in the radial direction which was expected for a side-pumped Nd:YAG rod with no end cooling employed. For end-pumped rods, the index of refraction would change in both the radial and axial direction. The incremental partition of the index of refractions in Table 3-2 are the same as the partitions of temperatures displayed in Table 3-1.

The user specified partition, selected for use in the Temperature Distribution Model, governs the partition of the Thermal Lensing Model. The partition of 10 equally spaced increments are normally chosen because it is more than adequate for first approximations. Increasing the number of partitions does increase the accuracy of the approximation. However, the time required to run the Temperature Distribution Model increases linearly as the number of partitions increases. Comparison of the temperature outputs for a partition of 10 and 20 equally spaced increments showed a mere 0.4 percent difference in the approxi-

mated temperatures.

Figure 3-4 illustrates the three types of pumping beam profiles used to pump a laser rod. All three types of pumping profiles can be used to end pump a rod. (Normally, only the circular and parabolic beam profiles are used to describe the distribution of heat deposition in side-pumped operations.)

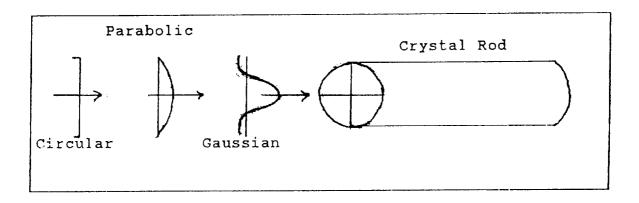


Figure 3-4. Types of Pump Beam Profiles

The above mentioned types of pump beam profiles have been implemented in the Temperature Distribution Model. In the thermal lensing ray-trace model, the focal length of the rod irrespective of the type of pumping beam used can be approximated. However, only the circular pump beam has been implemented for distortion calculations. Implementation of distortion calculations for parabolic and Gaussian beam profiles have been left as a future model enhancement. Table 3-1 represents a matrix of temperatures for a specif-

ic rod operating with user specified parameters. It serves as one of the primary inputs to the Thermal Lensing Model.

A radially dependent phase delay is experienced by a wave front propagating through a medium with a varying index of refraction n. Thus, a thin slab of the crystal medium can be approximated as a thin lens. The lensing model traces wave fronts propagating through the rod starting from several radial positions at the rod front face. the ray propagates through the rod, a series of thin lenses are setup and the temperature dependence of the index of refraction is calculated at specified locations. Using these calculations, a focal length associated with each tracing ray can be estimated. An average focal length for the rod is obtained by taking the mean of the focal lengths of the individual tracing rays. The specified axial increment of the temperature matrix determines the number of equivalent thin lens placed in series that the tracing ray must pass through. For example, with an axial incremental spacing of 0.1, as depicted in Table 3-1, 20 equivalent thin lens are placed in series from the front to the back of the rod.

A plane wave propagating through a lens-like medium acts as a spherical thin lens and diverges. Using this fact, the thin lens focal expression (3-11) was changed to:

$$f_r = -\frac{(rr_o)^2}{\Delta z L \sum [n_r(r,z) - n_o(0,z)]}$$
 (3-21)

where r_0 and r are the exiting relative radius of the ray and the radius of the rod in cm, respectively; z is the specified axial increment of the rod (dimensionless); L is the length of the rod in cm; and $n_r(r,z)$, $n_0(0,z)$ are the temperature dependent index of refraction for the radial point of interest and for the center of the rod, respectively. The focal length expression (3-21) can be applied upon determination of the quantities r_0 , $n_r(r,z)$, and $n_0(0,z)$. Calculating these scalar quantities are the essence of the thermal lensing ray-trace model.

The radial variation in temperature, as confirmed by use of curve fitting algorithms, is quadratic in nature. This fact allowed the selection and development of a binomial interpolation algorithm to obtain values of temperature at points other than the selected matrix points. The binomial interpolation algorithm is based on the approximation:

$$ax^2 + bx + c = T$$
 (3-22)

where a,b,and c are constant coefficients, x is either the radial (r) or axial (z) coordinate, and T is the temperature. By invoking this algorithm using a set of three collinear temperature (input) values along with their coordinate specifications, we can obtain a value for the temperature at any other point not specified in the temperature matrix.

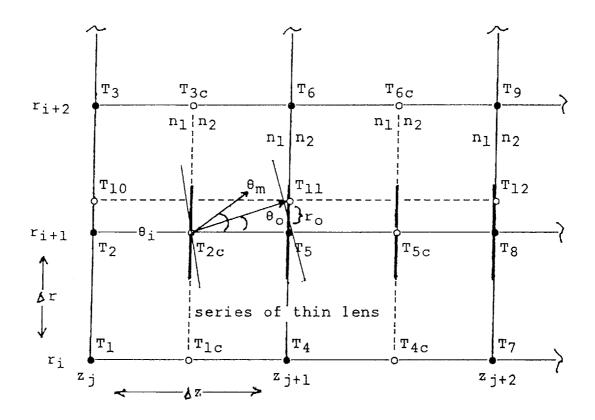


Figure 3-5. Partial Illustration of the Thermal Lensing Matrix With a Series of Thin Lens Overlaid

The temperature matrix (obtained from the input file) is illustrated in Figure 3-5. A wave front ray will be traced starting at the r_{i+1} radial input position through a series of equally spaced ($\Delta z/2$) thin lenses. The r_{i+1} ray was selected to illustrate the definition of the input and output angles that occur as the ray passes through a thin lens. These angles are necessary to calculate the exiting radius of the ray (r_0) for use in the focal length expression (3-21) and distortion calculations.

The r_1 ray (center of the rod) is also traced to ob-

tain a summation of the temperature variation of the index of refraction at the center of the rod, $n_0(0,z)$. As illustrated in Figure 3-5, temperatures T_1 through T_9 are obtained from the temperature matrix provided as input. Invoking the binomial interpolation algorithm allowed the calculation of the intermediate temperatures T_{1c} through T_{6c} for use in the thermal lensing scheme. This completes the basic setup of the thermal lensing scheme and provides the framework to proceed with the ray-tracing of specific input rays.

A collimated plane wave entering the rod will have an input angle (θ_i) equal to zero. As it passes through the first lens, the angle (θ_m) between the normal to the surface of constant temperature and the rod axis will be calculated at $\Delta z/2$. To calculate θ_m , we determine first the surface of constant temperature by obtaining the r and z derivatives of expression (3-22). The derivatives are given by:

$$\frac{dT(r)}{dr} = 2ar_i + b ag{3-23}$$

$$\frac{dT(z)}{dz} = 2a\left(\frac{\Delta z}{2}\right) + b$$
 [3-24]

where r_i is the input radius, Δz is the axial incremental spacing, and a,b are the calculated coefficients using the appropriate radial and axial temperature points in the in-

terpolation algorithm. The angle θ_m at $\Delta z/2$ is then calculated using the trigonometric expression:

$$\theta_{\rm m} = \tan^{-1} \left(\frac{{\rm d}r}{{\rm d}z} \right) \tag{3-25}$$

On finding the angle θ_m , the next step is to determine the specific values of the index of refraction on each side of the imagined lens. Due to the fact that the temperature dependent index of refraction changes very little between adjacent points (<< 1), it was decided to compute the index of refraction on each side of θ_m according to the following expressions:

$$n_1 = n_0 + \alpha \left(\frac{T_2 + T_m}{2} \right)$$
 [3-26]

$$n_2 = n_0 + \alpha \left(\frac{T_m + T_5}{2} \right)$$
 (3-27)

where n_0 is the index of refraction of the rod at its ambient temperature; α is the specified dn/dT of the rod; and T_2 , T_5 , and T_M (same as T_{2c} in the first stage of tracing) are the specific temperature points before, at, and after the position of the imagined lens.

By invoking Snell's law, the output angle (θ_0) of the ray passing through the thin lens can be obtained by substitution in the expression:

$$\theta_{o} = \theta_{m} - \sin^{-1} \left[\frac{n_{2}}{n_{1}} \sin(\theta_{m} - \theta_{i}) \right]$$
 (3-28)

After finding the output angle, the change in output radius (r_0) can be calculated from the trigonometric expression:

$$r_{o} = \frac{\Delta z}{2} \tan \theta_{o} + r_{m}$$
 (3-29)

where r_m is the midpoint radial position of the ray (same as r_{i+1} for initial entry of the ray into the rod). The output angle (θ_0) and output radius (r_0) are then sent to a recursive numerical algorithm to refine the output values at Δz to meet operator specified accuracy criteria for θ_0 .

The phase shift in the temperature variation of the index of refraction can be calculated, for the initial entry of the ray into the rod, and is proportional to the expression:

$$n_r(r,z) = n_1 + n_2 \sqrt{1 + \frac{(r_o - r_m)r}{(\frac{\Delta z}{2}L)^2}}$$
 (3-30)

and for later increments of the rod to:

$$n_{r}(r,z) = n_{1} \sqrt{1 + \frac{(r_{m} - r_{i})r}{(\frac{\Delta z}{2}L)^{2}} + n_{2} \sqrt{1 + \frac{(r_{o} - r_{m})r}{(\frac{\Delta z}{2}L)^{2}}}}$$
 [3-31]

The individual calculations from each lens, as the ray propagates through the rod, are retained and summed to determine the value for $n_r(r,z)$ which is then used in the focal length expression (3-21).

One-to one distortion mapping of a ray propagating through a lens-like medium is a straight forward calculation when dealing with side and end-pumped circular beams. The input irradiance (I) of the collimated plane wave is constant as it enters the crystal medium. The incremental change in irradiance is then calculated at the output end of the rod from the expression:

$$\Delta I = \frac{r_i^2(i+1) - r_i^2(i)}{r_o^2(i+1) - r_o^2(i)}$$
 [3-32]

where r_0 , r_i are the output and input radius of the ray being traced, respectively. The percentage of total distortion (D), for each ray, is then calculated from the expression:

$$D = 100 - \left(\frac{r_o^2(i+1) - r_i^2(i+1)}{r_i^2(i+1)}\right)$$
 [3-33]

This completes the formulation of the thermal lensing ray-trace model. Now, it's just a formality of computer record keeping to invoke the binomial interpolation algorithm, using r_0 , to calculate T_{10} , T_{11} , and T_{12} , reset

the output radius (r_0) of the previous rod segment equal to the input radius (r_i) of the next rod segment, reset the output angle (θ_0) equal to the input angle (θ_1) , and increment forward to the next imagined thin lens. The calculations are repeated until the ray exits the rod. When the ray exits the rod, the focal length and distortion associated with the ray are calculated and retained. Then, the ray-trace program increments upward in the matrix of temperatures to trace the next input ray. Upon completion of the ray tracing for a block of temperatures, the mean of the individual focal lengths and distortion present for that block of temperatures are then calculated. The model then increments forward to the next block of input temperatures (at a later time) and repeats the process until the input file of temperatures are exhausted and a time dependent average focal length are obtained.

The Thermal Lensing Model program code is contained in Appendix A. An example of the lensing model inputs and output are enclosed in Appendix B and C, respectively.

CHAPTER 4

Analysis and Discussion of Thermal Lensing

The next generation of solid-state lasers (used for remote sensing of the atmosphere from space platforms), are under development. Various new lasing materials and laser configuations are being investigated. Currently, the solid-state, end-pumped diode lasers are the most promising candidates due to their small size, reliability, performance, low power and cooling requirements, etc. Analyzing thermal lensing effects for these end-pumped configuations, using various cooling schemes are of interest to the designers of laser systems. Theoretical formulations, numerical calculations and experimental data do not exist for end-pumped configuations.

Before proceeding with the analysis of thermal lensing in end-pumped Nd:YAG and Ti:AL2O3 laser rods, an assessment of the validity of the Thermal Lensing Model was conducted. The validation was based on the comparison of model results with the experimental data for a repetitively pulsed side-pumped Nd:YAG laser. This case was interesting from two points. It was the only laser found, with actual experimental data on thermal focal length. The second point of interest is that the laser was side-pumped. The later point allowed for the extrapolation of Koechner's predic-

tion which are based on a CW side-pumped Nd:YAG laser.

Thus, the model results were compared to both the experimental results and Koechner's theoretical formulation for a long continuously side-pumped rod.

A. Model Validation.

Research of the literature shows that theoretical formulation and experimental data on thermal lensing effects do not exist for repetitive pulsed end-pumped lasers due to their recent development. In fact, very little data exist on repetitively pulsed side-pumped lasers. The vast majority of data published such as theoretical formulations, theoretical calculations, experimental results, etc. are based on CW side-pumped lasers dating back to the early 1970's. Most of these early analyses were conducted by Koechner^{5,9} and are still being referenced to as the authoritative source on the subject today.

A recent experiment, depicting the results of thermal focusing for a repetitive pulsed side-pumped Nd:YAG laser has been completed. 20 The laser rod used in the experiment had a length of 7.6cm, a radius of 25mm, was side-pumped uniformly, and cooled along its length (ends were not cooled). Each pump pulse had a duration of 130µs and an energy level of 10 Joules. Experimental calculations indicated that approximately 3.5 percent of the pump energy was absorbed into the rod as heat.

Both, the Temperature Distribution Model and Thermal Lensing Model were executed using the Nd:YAG material characteristics and the laser configuation of the experimental setup. The modeling and experimental results, along with Koechner's prediction of focal length from equation (3-18) are shown in Figure 4-1. (It should be noted that Koechner's prediction, used in Figure 4-1, did not include birefringence and bulge effects.)

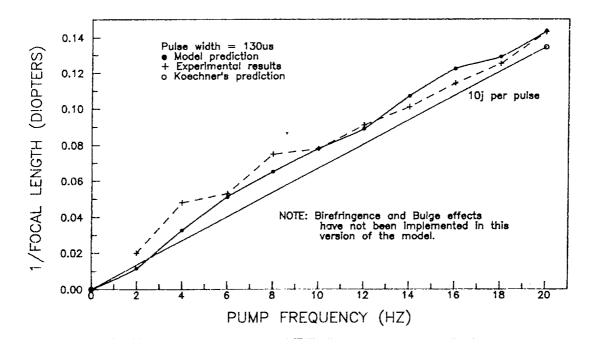


Figure 4-1. Thermal Focusing in Nd:YAG Rod

Figure 4-1 shows that the model's prediction of the thermal focal length are in good agreement with the experimental results and Koechner's theoretical prediction of focal length for an equivalent power problem. Thus, the ray-

trace model, based on the thermal gradients provided by the Temperature Distribution Model, will give a fairly accurate first order approximation.

Transient thermal focal length calculations of a side-pumped Nd:YAG rod do indicate an appreciable deviation from the standard steady-state power calculations using Koechner's prediction equation (3-18). Starting from an inactive condition, the Nd:YAG rod thermal focal length did stabilize at about 3.5 seconds. However, the steady-state calculations from the model at the end of each pump pulse indicates a higher focusing power of about 15-25 percent at frequencies of 4-20 hertz over the results as predicted by Koechner. This was not unexpected as the model was executed in an repetitive pulsed mode. Where as, Koechner's prediction are based on a thermally stabilized CW pulsed (same power) rod.

The transient side-pumped thermal focal length varies from 28 meters at 100ms to 6.97 meters at the steady-state equilibrium condition. The time dependent focal length, as shown in Figure 4-2, was computed at the end of each pump pulse for the above described laser rod. The rod was pumped by a 20 Hz, 10 Joule per pulse flash lamp. The horizontal line was obtained by using Koechner's formula for a thermally stabilized CW pulsed (same power) rod whose surface temperature was kept at a fixed value.

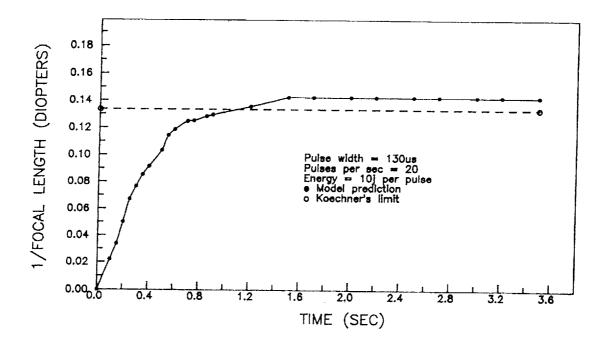


Figure 4-2. <u>Transient Thermal Focal Length for a Side-Pumped Nd:YAG Rod</u>

Thermally induced focusing varies significantly in the time interval between pulses. Even at a 10Hz repetition frequency, the variation in the Nd:YAG thermally induced focal length was approximately 10 percent.

The model was also used to estimate the impact of surface cooling on the focal length. Focal length was found to be very sensitive in the low end of the surface cooling parameter. Figure 4-3 displays the results of focal length versus cooling in side-pumped Nd:YAG rods. The cooling parameter is a dimensionless quantity obtained by multiplying the length of the rod by the surface heat transfer

coefficient and dividing by the bulk thermal conductivity of the rod material. Koechner's formulation, by comparison, is for a fixed surface temperature.

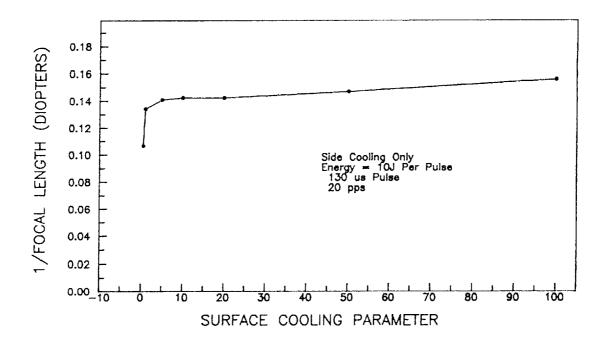


Figure 4-3. Focal Length vs Cooling in Side-Pumped Nd:YAG Rod

Figure 4-3 is also important to system designs. It shows that above a certain point, very little is gained from additional cooling. Therefore, the most efficient cooling for the laser is critical for spaced based applications. Power consumption in space platforms are one of the most critical design parameters. Additional unneeded cooling may strain the limited power resources available in space.

One-to-one mapping of intensity in the repetitive pulsed side-pumped Nd:YAG laser showed distortion to be negligible during the rod transient period. This result was expected due to the presence of only radial thermal gradients (no axial gradients) as a result of the uniform pumping of the rod and the absence of end-cooling.

B. Analysis of Thermal Lensing in End-Pumped Nd:YAG and Ti:AL₂O₃ Laser Rods.

Thermal lensing calculations have been obtained for the two end-pumped laser rod configuations depicted in Table 4-1 below. Both of these laser crystals are currently undergoing feasibility experiments in the laboratory at NASA Langley Research Center. It should be noted here that the comparison is not between crystals of different dimensions, but between crystals of practical dimensions. Both

Table 4-1. End-Pumped Laser Rod Characteristics

Parameters	Nd:YAG	Ti:AL ₂ O ₃
Rod Length (cm) Rod Radius (cm) Thermal Diffusivity (cm ² /s) Thermal Conductivity (W/cm ^O K) Material dn/dt Index of Refraction Optical Attenuation Pump Wavelength (microns) Pump Energy Absorbed (J/cm ³) Pump Pulse Duration (seconds)	1.0 0.4 26.947 0.103 8.9x10-6 1.825 3.0 1.15 0.050 0.010	0.6 0.2 8.87 0.330 1.28x10 ⁻⁵ 1.7654 3.0 0.6438 0.050 0.010

crystals were end-pumped by a Gaussian beam where the ratio

of the beamwidth to the rod radius is 0.5. With the exception of the rod material characteristics, all other parameters such as side and end cooling, energy absorbed, pump pulse duration, etc. were the same for both rods. Both, the Temperature Distribution Model and the Thermal Lensing Model were executed using the appropriate material characteristics of the rod and the laser configuation depicted in Table 4-1.

Figures 4-4 and 4-5 presents the single pulse transient behavior of thermal focal length for Nd:YAG and Ti:AL₂O₃ crystals, respectively. Both rods were end-pumped

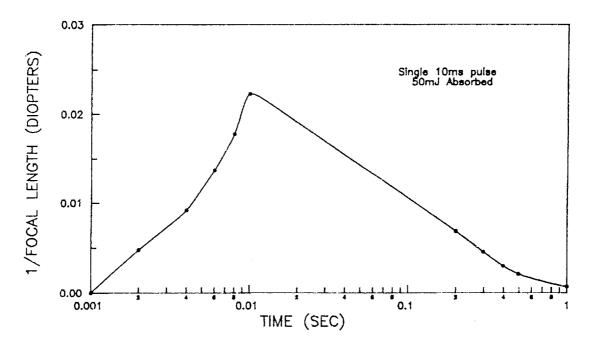


Figure 4-4. Single Pulse Transient of Thermal Focal Length in Nd:YAG Crystal

with a single pulse of 10ms duration. The energy absorbed

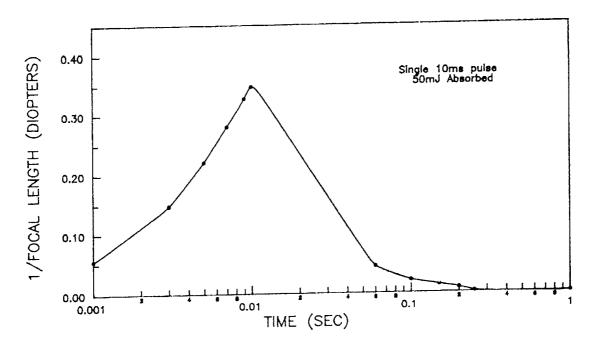


Figure 4-5. Single Pulse Transient of Thermal Focal Length in Ti:AL2O3 Crystal

into the rod as heat was assumed to be 50mJ per pulse. Moderate side cooling parameter of 20 was employed. Ends were not cooled. (The cooling parameter is a dimensionless quantity obtained by multiplying the length of the rod by the surface heat transfer coefficient and dividing by the bulk thermal conductivity of the rod material.) Starting from an inactive condition, the thermal focal length for Nd:YAG ranged from 205 meters at 2ms to the minimum of 44.8 meters at 10ms when the pump pulse was turned off. For Ti:AL2O3, the thermal focal length ranged from 18 meters at 1ms to 2.87 meters at 10ms. Although some residual heat still exist in the rods, as the rods relaxes to its ambient

condition, the thermal focal lengths are no longer measurable 1.30 seconds and 250ms after pump shutdown for Nd:YAG and $\text{Ti:AL}_2\text{O}_3$ rods, respectively. For all practical purposes, as far as focal length is concerned, the rods have returned to their ambient state at this point.

The transient thermal focal length profiles for Nd:YAG and $Ti:AL_2O_3$ during multiple pulse operations are shown in Figures 4-6 and 4-7. As seen in Figure 4-6, the Nd:YAG rod

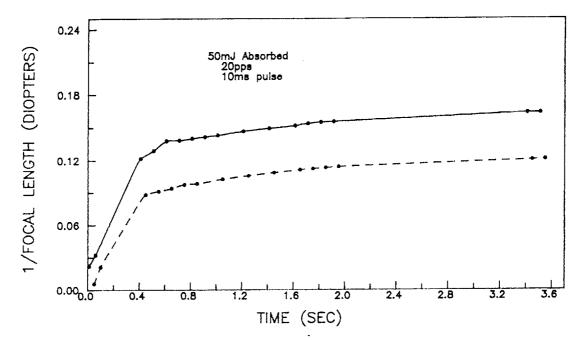


Figure 4-6. Transient Thermal Focal Length for a Multiple Pulsed, End-Pump Nd:YAG Rod

thermal focal length stabilized at about 3.5 seconds. For ${\rm Ti:AL_2O_3}$, the rod thermal focal length stabilized at about 300ms. In both rods, it was found that the thermal focal lengths stabilized at the same time the temperatures became

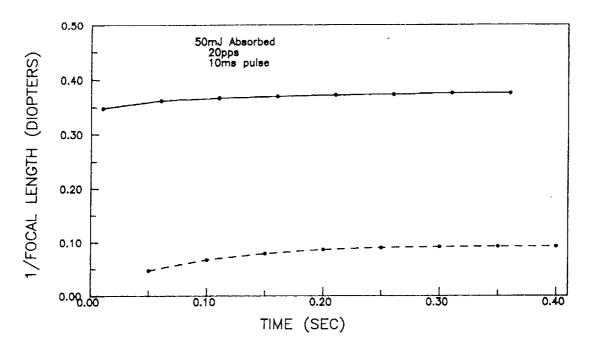


Figure 4-7. Transient Thermal Focal length for a Multiple Pulsed, End-pumped Ti:AL₂O₃ Rod

stabilized which was expected. The Nd:YAG transient endpumped thermal focal length varied from 44 meters at 10ms
to 6.11 meters at the steady-state equilibrium condition.
For Ti:AL2O3, the thermal focal length varied from 2.87 meters at 10ms to 2.66 meters at steady-state equilibrium.
These time dependent focal lengths, shown in the solid
lines, in Figures 4-6 and 4-7 were computed at the end of
each pump pulse for the described laser rods. Both rods
were pumped at a 20 Hz rate. Energy absorbed into the rods
as heat was assumed to be 50 mJ per pulse.

Thermally induced focusing varied significantly in the

time interval between pulses as shown by the dashed lines in Figures 4-6 and 4-7. The variation was approximately 26 and 75 percent for Nd:YAG and Ti:AL2O3, respectively. The time dependent focal length between pulses were computed at the start of each pump pulse for the above rods. Not accounting for the temporal variation of the thermally induced focal length during the pulse relaxation period, may lead to significant errors during design.

The next factor looked at was thermal focusing versus pump frequency and the impact of side and end cooling on thermal focal lengths. Figures 4-8 and 4-9 depict the results for Nd:YAG and Ti:AL₂O₃, respectively. Pump frequen-

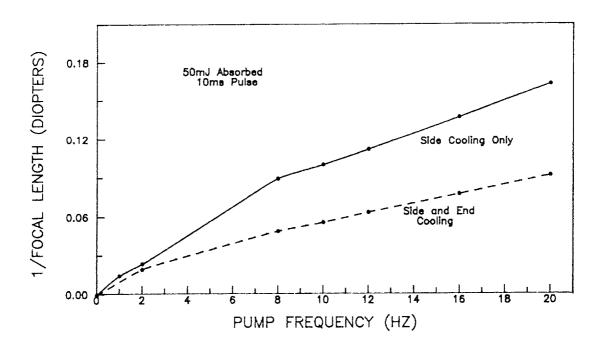


Figure 4-8. Thermal Focusing in End-Pumped Nd:YAG Rod

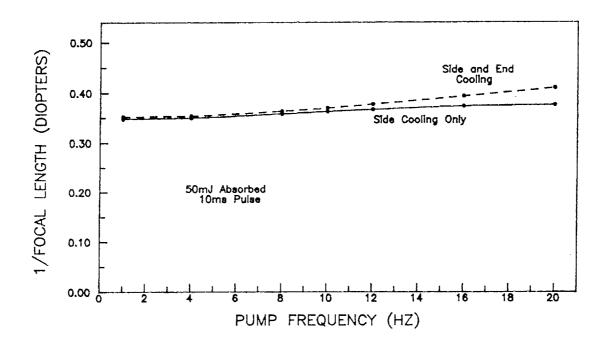


Figure 4-9. Thermal Focusing in End-Pumped Ti:AL₂O₃ Rod

cy was varied between 1 and 20 HZ. For each frequency, the rod was allowed to stabilize (3.5s for Nd:YAG and 300ms for Ti:AL₂O₃) before calculations were made. In both figures, moderate side cooling parameter of 20 was employed. For calculations involving both side and end cooling, end cooling was set equal to the side cooling. As shown in Figure 4-8, the impact of end cooling caused a significant decrease in the Nd:YAG thermal focal length above 2 Hz. This result was expected as the radial and axial temperature gradients near the rod ends become smoother due to end cooling.

For Ti:AL₂O₃, very little impact from end cooling was experienced until the 12 HZ pump frequency was reached. However, in comparison to Nd:YAG where the thermal focal length was significantly decreased, the opposite effect was obtained for Ti:AL₂O₃. End cooling of Ti:AL₂O₃ crystals causes small increases in the thermal focal length as the pump frequency is increased. This result was not expected. However, upon further analysis of the temperature profiles for Ti:AL₂O₃, it was apparent that the radial and axial temperature gradients near the ends were greater due to end cooling.

Finally, the model was used to estimate the impact of surface cooling on the induced thermal focal lengths for end-pumped Nd:YAG and Ti:AL2O3 laser crystals. The rods were pumped at a 20 HZ rate and energy absorbed into the rod as heat was assumed at 50mJ per pulse. Figures 4-10 and 4-11 presents the results of focal length versus side cooling for these configuations. The focal length was found to be very sensitive only on the low end of the surface cooling parameter for both rods. Therefore, sizing end-pumped lasers for correct cooling is critical for spaced based applications as previously explained.

Distortion calculations were not performed on these end-pumped lasers as the function for mapping of Gaussian beams has not been implemented in the model (left as a fu-

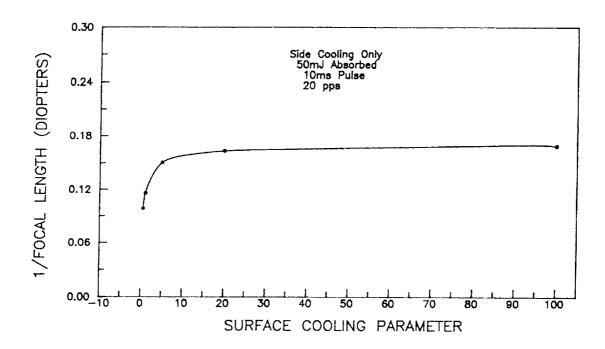


Figure 4-10. Focal Length vs Side Cooling in End-Pumped Nd:YAG Rod

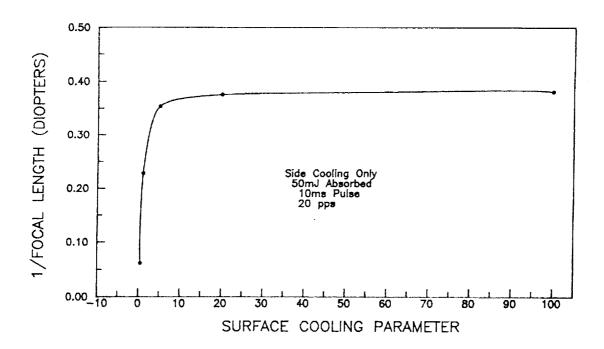


Figure 4-11. Focal Length vs Side Cooling in End-Pumped Ti:AL2O3 Rod

ture model enhancement). Unlike the side-pumped configuation, previously discussed, where distortion was non-existent at thermal equilibrium, preliminary indications are that distortion in the end-pumped configuations will be on the order of 3-5 percent at thermal equilibrium.

CHAPTER 5

Summary and Conclusions

An analytic expression for approximating the time-dependent thermal focal length in finite solid-state laser rods has been derived. The analysis is based on the temperature variation of the material refractive index caused by optical pumping of these rods. This analysis is also applicable to situations where the laser rod is side or end-pumped by circular, parabolic, or Guassian beam profiles. Short or long pulse, continuous wave (CW), or repetitive pulsed operations are also applicable. The repetitive pulsed, end-pumped solid-state diode laser configuations are of current research interest as the next generation of lasers will come from this category.

Several quantities were found to be relevant to this analysis. These quantities were the specific thermal profiles of the rods, type of optical pumping employed, type of cooling scheme employed (side and end-cooling parameters), and the specific material characteristics of the rods.

The Thermal Lensing Model was formulated using geometric ray tracing based on the focal length expression for a thin lens. The focal lengths are then approximated, by calculating the phase shift in the index of refraction, as

the plane wave is tracked through a lens-like crystal medium.

Thermally induced temperature profiles, for end-pumped laser rods operating with specified parameters, are approximated by the Temperature Distribution Model. These thermal profiles are then inputted to the developed Thermal Lensing Model. The Thermal Lensing Model is then used to approximate the transient thermal focal length and estimate the final rise in thermal focal length for the laser rod under evaluation. Various pumping and cooling schemes can be evaluated for their effect on the induced thermal focal length. For circular pump beam profiles, distortion calculations are also approximated by the model.

The numerical examples for end-pumped, repetitively pulsed Nd:YAG and ${\tt Ti:AL}_2{\tt O}_3$ laser rods showed the following major results.

- a. The minimum induced thermal focal length is achieved at the time of pump pulse turn off for both rods operating under single long pulse conditions.
- b. For multiple pulse operations, the minimum induced thermal focal length was achieved when the rod reached its thermal equilibrium condition (3.5 seconds for Nd:YAG and 300ms for Ti:AL₂O₃).

- c. Thermally induced focusing varied significantly in the time interval between pulses (26 percent for Nd:YAG and 75 percent for Ti:-AL₂O₃).
- d. Employment of end-cooling significantly decreased thermal focusing in Nd:YAG above the 2 Hz pump frequency. For Ti:AL₂O₃, the opposite effect was found. Small increases were noticed in the thermal focal length for pump frequencies above 12 Hz.
- e. Under conditions when only the side cooling was varied, the induced thermal focal length was found to be very sensitive at the low end of the scale for both rods.

The model was validated against experimental data and theoretical calculations of thermal focal length for a repetitive pulsed, side-pumped Nd:YAG laser. It is seen that the prediction of thermal focal length is in good quantitative agreement with experimentally observed behavior. Thus, the Thermal Lensing Model, based on the thermal profiles provided by the Temperature Distribution Model, will give a fairly accurate first order approximation of the thermal focal length.

Appendix A

Computer Program Listing

1. Functional Description

The Thermal Lensing Model (THERLENS.FOR) is not a standalone computer program. Its primary input is dependent on the output of a previously developed theoretical model titled: Temperature Distribution Model for finite optically pumped laser rods. The output of the Temperature Distribution Model (blocks of temperature data versus time), along with other thermal lensing constants (see Appendix B), are inputted to the lensing model. The model then calculates the finite changes in focal length and distortion effects due to the temperature gradients within the laser rod. Appendix C depicts the Thermal Lensing Model output.

Currently, the lensing model can calculate the thermal lensing effects for side and end-pump configurations and distortion approximations for circular pump beams only.

(Note: Distortion calculations for parabolic and Gaussian pump beams will be implemented in the future.) The optical axis of the laser rod is assumed to be along the axis of the rod.

2. Environmental Characteristics

This program was written in the Fortran language. It was compiled and linked using the Microsoft Fortran 77

Optimizing Compiler Version 4.10. The Thermal Lensing Model can be executed on any IBM/IBM compatible 286/386AT micro-computer with a 287/387 Math Coprocessor. This version can also be executed on the VAX 750 mini-computer. The source program size on the AT-machine is 46,527 bytes and the executable program is 69,621 bytes. The enclosed program code contains all changes through March 1, 1990.

3. Thermal Lensing Program Listing

(Program listing starts on next page)

Thermal Lensing Program Listing

03-01-90 18:42:07

Microsoft FORTRAN Optimizing Compiler Version 4.10 Source Line 1 SDEBUG A COMPUTER PROGRAM SIMULATION MODEL TO COMPUTE THERMAL LENSING FROM 3 C TEMPERATURE DISTRIBUTION PROFILES IN OPTICALLY PUMPED LASER CRYSTAL 4 C 5 C RODS. (YY.FOR) 6 ******************** 7 C 8 С Version 1.0 9 C THERLENS.FOR: Language: Microsoft Fortran77 Version 4.10 10 C 11 C Vincent G. Brackett 12 C Written by: Graduate Student Applied Mathematics 13 C Hampton University 14 C Hampton, Va. 23668 15 C 16 C Thesis Advisor: Dr. Usamah O. Farrukh 17 C Department of Engineering 18 C Hampton University 19 C 20 C NASA Langley Research Center For: 21 C Hampton, Va. 23666 22 C 23 C GRANT: NAG 1-666 24 C Philip Brockman 25 C Monitor: 26 C Last Revised: March 1, 1990 27 C Date: 28 C ************************ 29 C 30 C 31 C THIS PROGRAM USES THE TEMPERATURE OUTPUT PROFILES OF A PREVIOUSLY 32 C DEVELOPED COMPUTER SIMULATION MODEL (THAT MODEL PREDICTS THE 33 C NORMALIZED TEMPERATURE DISTRIBUTIONS VERSUS TIME IN FINITE SIDE AND END-PUMPED LASER CRYSTAL RODS) TO PREDICT THERMAL LENSING (FINITE 35 C CHANGE IN FOCAL LENGTHS) CAUSED BY THE RESULTANT TEMP GRADIENTS IN 36 C THOSE RODS. THERMAL DISTORTION OF THE PUMP BEAM ARE CALC AND AVG 37 C VALUES OF THE FOCAL LENGTHS AND DISTORTION ARE PRESENTED. 38 C 39 C CAUTION: The matrix mesh of the Temperature Distribution Model and 40 C this model must be the same size. To change matrix mesh 41 C

42 C 43 C size, only the parameter statement needs to be changed.

```
PARAMETER (N=11, M=11)
44
45 C
          DIMENSION TEMP(N,M), INDEX(N,M), RAD(M), LON(N), DISTOR(M)
46
          DIMENSION ANGI(M), ANGM(M), ANGO(M), REND(M), FOCAL(M)
47
48 C
          REAL LAMBDA, LAMBDL, K, LRMIN, LRMAX, LR, LENG, LON, IOR, INDEX, N1, N2, LONI
49
50 C
          DOUBLE PRECISION PI, SUMIOR, SUMINT, SIORO, SIORJ, SINTJ, ANGIJ, ANGOJ
51
52
          DOUBLE PRECISION RI, RM, RO, Z, A, B, C
53 C
54
          CHARACTER*1 XX(140)
55 C
          COMMON /BLOCK1/IOR, DT, ACC, N1, N2, ZI, RI, RM, TM, LONI, I
56
57
          COMMON /BLOCK2/R1, R2, R3, Z1, Z2, Z3
          COMMON /BLOCK3/T1.T2,T3,T4,T5,T6,T7,T8,T9
58
          COMMON /BLOCK4/T1C, T2C, T3C, T4C, T5C, T6C, T10, T11, T12
59
60 C
          OPEN(4,FILE='THERLEN1.INP',STATUS='OLD')
61
          OPEN(5, FILE='THERLEN2.INP', STATUS='OLD')
62
          OPEN(6, FILE= 'THERLENS.OUT', STATUS= 'UNKNOWN')
63
64 C
                               ... (PROCESSING OF INPUT FILE ONE)...
65 C
66 C
          WRITE(6,*)' '
67
                        ..... THERMAL LENSING OUTPUT FILE.....
          WRITE(6,*)'
68
          WRITE(6,*)'
69
                         WRITE(6,*)'
70
          WRITE(6,*)'
71
          READ(4,'(80A1)') (XX(I), I=1,80)
72
73
          WRITE(6,*) (XX(I), I=1,80)
          READ(4,'(80A1)') (XX(I), I=1,80)
74
75
          WRITE(6,*) (XX(I),I=1,80)
76
          READ(4,*) WL
          WRITE(6,*) '.. WAVELENGTH OF INTEREST IN UM.. (WL).: ',WL
77
78
          READ(4,*)TOI
          WRITE(6,*)'..TEMPERATURE OF INTEREST IN DEG C..(TOI).: ',TOI
79
          READ(4,*) IOR
80
          WRITE(6,*) '..INDEX OF REFRACTION..(IOR).: ',IOR
81
82
          READ(4,*) DT
83
          WRITE(6,*) '..ALPHA (dn/dt)..(DT).: ',DT
84
          READ(4,*) TNF
          WRITE(6,*) '.. TEMP NORMALIZATION FACTOR..(TNF).: ',TNF
85
          READ(4,*) TINF
86
          WRITE(6,*) '.. TIME NORMALIZATION FACTOR..(TINF).: ', TINF
87
88
          READ(4,*) IDATA
          WRITE(6,*) '..0=RELATIVE TEMP; 1=ACTUAL TEMP..(IDATA).: ',IDATA
89
          READ(4,*) ZI
90
          WRITE(6,*) '..AXIAL INCREMENT FACTOR..(ZI).: ',ZI
91
92
          READ(4,*) POWER
          WRITE(6,*) '.. POWER MULTIPLICATION FACTOR.. (POWER) .: ', POWER
93
94
          READ(4,*) ACC
```

```
WRITE(6,*)'..OUTPUT ANGLE ACCURACY CRITERIA..(ACC).:', ACC
95
          READ(4,*) TPUMP
96
          \label{eq:write} \texttt{WRITE}(\texttt{6}, \texttt{\star}) \text{ '...} \texttt{TYPE OF PUMPING (0=side, 1=end)...'}, \texttt{TPUMP}
 97
          WRITE(6,*) '-----
98
          WRITE(6,*) '-----
99
100 C
                              ...(PROCESSING OF INPUT FILE TWO)...
101 C
102 C
          WRITE(6,*)'
103
                       ......INPUT FILE #2......
          WRITE(6,*)'
104
          WRITE(6,*)
105
           JJ=0
106
         5 CONTINUE
107
           IF((JJ/3)*3.NE.JJ) GOTO 10
108
           READ(5,100,ERR=86) (XX(I),I=1,132)
109
           WRITE(6,100) (XX(I), I=1,132)
110
        10 CONTINUE
111
112 C
           IF(JJ.NE.O) GO TO 20
113
           IF(TPUMP.EQ.0) THEN
114
           DO 15 J=1,80
115
           READ(5,100,ERR=87) (XX(1),I=1,132)
116
           WRITE(6,100) (XX(I),I=1,132)
117
118
        15 CONTINUE
           ELSEIF(TPUMP.EQ.1) THEN
119
           DO 16 J=1,81
120
           READ(5,100,ERR=87) (XX(1),I=1,132)
121
           WRITE(6,100) (XX(I), I=1,132)
122
123
        16 CONTINUE
           ENDIF
124
125 C
        20 JJ=JJ+1
126
           P=P+1
127
           READ(5,100,ERR=88) (XX(I),I=1,132)
128
           WRITE(6,*)' BLOCK OF TEMPERATURE PROFILES FROM INPUT FILE #2'
129
           READ(5,100) (XX(I), I=1,132)
130
           WRITE(6,100) (XX(I),I=1,132)
131
            READ(5,100) (XX(I), I=1,132)
132
           WRITE(6,100) (XX(1),I=1,132)
133
            READ(5,105) (XX(I), I=1,50), DIFF
134
           WRITE(6,105) (XX(I),I=1,50),DIFF
135
            READ(5,105) (XX(I),I=1,50),RADI
136
           WRITE(6,105) (XX(I), I=1,50), RADI
137
            READ(5,105) (XX(I),I=1,50),LENG
138
            WRITE(6,105) (XX(I), I=1,50), LENG
139
            READ(5,105) (XX(I),I=1,50),SEC
140
            WRITE(6,105) (XX(I),I=1,50),SEC
<sup>-</sup>141
 142 C
            DO 25 J=1,2
 143
            READ(5,100) (XX(I), I=1,132)
 144
```

```
145
              WRITE(6,100) (XX(I), I=1,132)
   146
           25 CONTINUE
   147
   148
              READ(5,115) (XX(I),I=1,7),(LON(I),I=1,N)
   149
              WRITE(6,115) (XX(I),I=1,7),(LON(I),I=1,N)
  150 C
  151
              DO 30 J=1.M
  152
             READ(5,125) (XX(I), I=1,2), RAD(J), (TEMP(I,J), I=1,N)
             WRITE(6,125) (XX(I), I=1,2), RAD(J), (TEMP(I,J), I=1,N)
  153
  154
          30 CONTINUE
  155
             DO 40 J=1,M
  156
             DO 35 I=1.N
  157
             TEMP(I, J)=TEMP(I, J)*POWER
  158
             IF(IDATA.EQ.0) TEMP(I,J)=TEMP(I,J)*TNF
  159
          35 CONTINUE
  160
          40 CONTINUE
  161
             WRITE(6,*)'
 162
             WRITE(6,*)'
                                                THERMAL LENSING PROGRAM OUTPUT DATA'
  163
             WRITE(6,*)'
 164
             WRITE(6,*)'
                                                        INDEX OF REFRACTION MATRIX '
 165
             WRITE(6,*)'
 166
            DO 50 J=1,M
 167
             DO 45 I=1,N
 168
            INDEX(I,J) = IOR + (DT*TEMP(I,J))
 169
         45 CONTINUE
 170
            WRITE(6,125) (XX(I),I=1,2),RAD(J),(INDEX(I,J),I=1,N)
 171
         50 CONTINUE
 172 C
 173 C
                              ... (CALC OF LENSING AND DISTORTION)...
 174 C
 175
            PI=3.141592653589793D00
 176
            AREA=PI*ZI**2
177
            SIORO=0
178
            DO 60 J=1,M-1
179
            ANGIJ=0.0D00
180
            SIORJ=0.0D00
181
           SINTJ=0.0D00
182
           DO 55 I=1,N-1
183
           IF(I.EQ.10) GOTO 65
184
           IF(J.EQ.1) R1=-RAD(J+1)
185
           IF(J.GT.1) R1=RAD(J-1)
186
           R2=RAD(J)
187
           R3=RAD(J+1)
188
           IF(J.EQ.1) Tl=TEMP(I,J+1)
189
           IF(J.GT.1) T1=TEMP(I,J-1)
190
           IF(J.EQ.1) T4=TEMP(I+1,J+1)
191
           IF(J.GT.1) T4=TEMP(I+1,J-1)
192
           IF(J.EQ.1) T7=TEMP(I+2,J+1)
193
           IF(J.GT.1) T7=TEMP(I+2,J-1)
194
           T2=TEMP(I,J)
```

```
195
           T5=TEMP(I+1,J)
           T8=TEMP(I+2,J)
196
           T3=TEMP(I,J+1)
197
           T6=TEMP(I+1,J+1)
198
           T9=TEMP(I+2,J+1)
199
           Z1=LON(I)
200
           Z2=LON(I+1)
201
           Z3=LON(I+2)
202
           Z=LON(I)+(ZI/2)
203
           CALL INTERP(Z,Z1,Z2,Z3,T,T1,T4,T7,A,B,C)
204
205
           T1C=T
           CALL INTERP(Z,Z1,Z2,Z3,T,T2,T5,T8,A,B,C)
206
           T2C=T
207
           CALL INTERP(Z,Z1,Z2,Z3,T,T3,T6,T9,A,B,C)
208
           T3C=T
209
           Z=LON(I+1)+(ZI/2)
210
            CALL INTERP(Z,Z1,Z2,Z3,T,T1,T4,T7,A,B,C)
211
            T4C=T
212
            CALL INTERP(Z,Z1,Z2,Z3,T,T2,T5,T8,A,B,C)
213
214
            T5C=T
            CALL INTERP(Z,Z1,Z2,Z3,T,T3,T6,T9,A,B,C)
215
           T6C=T
216
        65 CONTINUE
217
           LONI=LON(I)
218
219
            IF(1.EQ.1)THEN
220
                    CALL INITIAL (RO, ANGOJ)
                     SUMIOR=N1+N2*SQRT(1+((((RO-RM)*RADI)/(ZI/2*LENG))**2))
221
                    SIORJ=SIORJ+SUMIOR
222
                     IF(J.EQ.1) SIOR0=SIORJ
223
                     CALL MIDPT(RO, ANGOJ)
224
            ELSEIF(I.LT.N-1) THEN
225
                     CALL FINAL (RO, ANGOJ)
226
                     SUMIOR=N1*SQRT(1+((((RM-RI)*RADI)/(ZI/2*LENG))**2)) +
227
                           N2*SQRT(1+(((RO-RM)*RADI)/(ZI/2*LENG))**2))
228
           1
                     SIORJ=SIORJ+SUMIOR
229
                     IF(J.EQ.1) SIORO=SIORJ
230
                     CALL MIDPT(RO, ANGOJ)
231
            ELSEIF(I.EQ.N-1) THEN
232
                     CALL FINAL (RO, ANGOJ)
233
                     REND(J)=RO
234
                     SUMIOR=N1*SQRT(1+((((RM-RI)*RADI)/(ZI/2*LENG))**2)) +
 235
                           N2*SQRT(1+((((RO-RM)*RADI)/(ZI/2*LENG))**2))
236
           1
                     SIORJ=SIORJ+SUMIOR
237
                     N1=N2
238
                     IF(J.EQ.1) THEN
 239
                          DISTOR(J)=0
 240
                     ELSEIF(J.GT.1) THEN
 241
                          DISTOR(J)=100*((RO**2-R2**2)/R2**2)
 242
                     ANGO(J) = ASIN(N1*SIN(ANGOJ))
 243
                     ENDIF
 244
```

```
245
                     IF(J.EO.1) SIORO=SIORJ
 246
                    IF(SIORJ-SIORO.EQ.O) THEN
 247
                         FOCAL(J)=0
 248
                    ELSEIF(SIORJ-SIORO.NE.O) THEN
 249
                         FOCAL(J)=-(RO*RADI)**2/(ZI*LENG*(SIORJ-SIORO))
 250
                    ENDIF
 251
            ENDIF
 252
         55 CONTINUE
 253
         60 CONTINUE
 254
            WRITE(6,*)'
 255
            WRITE(6,*)'
 256
           WRITE(6,135) WL, TOI, SEC
 257
            WRITE(6,*)'
 258
           WRITE(6,*)'
                               RAY ANGLE OUT
                                                       RADIUS
                                                                    FOCAL '
 259
           1
                                DISTORTION '
260
           WRITE(6,*)'
                               (no.) (radians)
                                                        (cm)
                                                                    LENG(cm)'
 261
                                           (%)'
262
           WRITE(6,*)'
263
          1
264
           DO 70 J=1,M
265
           WRITE(6,130) RAD(J), ANGO(J), REND(J), FOCAL(J), DISTOR(J)
266
        70 CONTINUE
267
           WRITE(6,*)'
268
           AFOCAL=0
269
           DO 75 J=1,M
270
           AFOCAL=AFOCAL+FOCAL(J)
271
        75 CONTINUE
272
          IF(AFOCAL.EQ.O) GOTO 76
273
           AFOCAL=AFOCAL/(M-2)
274
        76 CONTINUE
275
        ADISTOR=0
276
           DO 80 J=1,M
277
           IF(DISTOR(J).GT.ADISTOR) ADISTOR=DISTOR(J)
278
        80 CONTINUE
279
           WRITE(6,140) AFOCAL/100
280
           WRITE(6,145) ADISTOR
281
           WRITE(6,*)' '
282
           WRITE(6,*)'
                                       .. END THERMAL LENSING OUTPUT..'
           WRITE(6,*)'.....
283
           WRITE(6,*)' '
284
285
           IF(AFOCAL.EQ.0) THEN
286
                  IF(P.GT.1) THEN
287
                     WRITE(6,*)'...PROGRAM TERMINATED. LASER ROD HAS ESSENTIALY',
                                ' RELAXED TO STATIC CONDITIONS.'
288
          1
289
                     GOTO 90
290
                  ENDIF
291
           ENDIF
292
          GOTO 5
293
        86 CONTINUE
          WRITE(6,*) ' ERROR ON LINE 109'
294
295
          GOTO 90
```

```
87 CONTINUE
296
                          ERROR ON LINE 116/121'
           WRITE(6,*) '
297
           GOTO 90
298
        88 CONTINUE
299
           WRITE(6,*) '
                          ERROR ON LINE 127'
300
301 C
       100 FORMAT(132A1)
302
       105 FORMAT(50A1,E11.6)
303
       115 FORMAT(7A1,14F12.2)
304
       125 FORMAT(2A1,F5.2,14E12.5)
305
       130 FORMAT(7X,F5.2,17E15.7)
306
       135 FORMAT(//,22X, THERMAL LENSING CALCUATIONS',
307
                                                             ',E12.6,
                   /,15X,'WAVELENGTH OF INTEREST(um).....
          1
308
                   /,15x, TEMPERATURE OF INTEREST(deg C).. ',E12.6,
          1
309
                   /,15X,'TIME (sec).....',E12.6)
          1
310
       140 FORMAT(7X, 'AVERAGE OF THE FOCAL LENGTHS (meters) = ',E15.6)
311
       145 FORMAT(7X, 'INCREMENTAL DISTORTION (%) RANGES FROM 0.0 TO ',E10.3)
312
313 C
314
        90 CONTINUE
           END
315
316 C
317 C
           SUBROUTINE INITIAL(RO, ANGOJ)
318
319 C
320 C
           This subroutine calculates the initial entry into the temperature
321 C
            gradient matix and perdicts the initial angle and radius out for
322 C
           the first axial increment of the laser rod.
323 C
324 C
           REAL IOR, LONI, N1, N2
325
326 C
            DOUBLE PRECISION ANGMJ, ANGIJ, ANGOJ, A1, A2, A3, RI, RM, RO, Z, A, B, C
327
328 C
            COMMON /BLOCK1/IOR, DT, ACC, N1, N2, ZI, RI, RM, TM, LONI, I
329
            COMMON /BLOCK2/R1,R2,R3,Z1,Z2,Z3
 330
            COMMON /BLOCK3/T1,T2,T3,T4,T5,T6,T7,T8,T9
 331
            COMMON /BLOCK4/T1C, T2C, T3C, T4C, T5C, T6C, T10, T11, T12
 332
 333 C
 334
            CALL INTERP(RI,R1,R2,R3,T,T1C,T2C,T3C,A,B,C)
 335
            DTR=(2*A*RI)+B
 336
            Z=LONI+ZI/2
 337
            CALL INTERP(Z,Z1,Z2,Z3,T,T2,T5,T8,A,B,C)
 338
            DTZ = (2*A*Z) + B
 339
            IF(DTR.EQ.0) THEN
 340
                   ANGMJ=0.0D00
 341
            ELSEIF(DTR.NE.O) THEN
 342
                   ANGMJ=ASIN(1.0)
 343
 344
            ENDIF
            IF(DTZ.GE.1.0E-30) ANGMJ=ATAN(DTR/DTZ)
 345
```

=

```
346
            RM=R2
347
            TM=T2C
            N1=IOR+DT*((TM+T2)/2)
348
349
            N2=IOR+DT*((TM+T5)/2)
350
            Al=SIN(ANGMJ-ANGIJ)
351
            A2=(N2/N1)*A1
352
            A3=ASIN(A2)
            ANGOJ=ANGMJ-A3
353
354 C
            ANGOJ=ANGMJ-ASIN((N2/N1)*SIN(ANGMJ-ANGIJ))
355
            RO=(ZI/2)*TAN(ANGOJ)+RM
356
            CALL REFINE(RO, ANGIJ, ANGMJ, ANGOJ, T4, T5, T6)
357 C
358
            RETURN
            END
359
360 C
361 C
362
            SUBROUTINE MIDPT(RO, ANGOJ)
363 C
364 C
            This subroutine calculates the intermediate angles and predicts
365 C
            the mid-point position of the next axial increment prior to
366 C
            entry into the next increment of the temperature gradient matrix.
367 C
368
           REAL IOR, LONI, N1, N2
369 C
370
           DOUBLE PRECISION ANGMJ, ANGIJ, ANGOJ, Al, A2, A3, RI, RM, RO, Z, A, B, C
371 C
372
           COMMON /BLOCK1/IOR, DT, ACC, N1, N2, ZI, RI, RM, TM, LONI, I
373
            COMMON /BLOCK2/R1,R2,R3,Z1,Z2,Z3
374
           COMMON /BLOCK3/T1,T2,T3,T4,T5,T6,T7,T8,T9
375
            COMMON /BLOCK4/T1C, T2C, T3C, T4C, T5C, T6C, T10, T11, T12
376 C
377
378
           RM=RO
379
            ANGIJ=ANGOJ
380
           CALL INTERP(RM,R1,R2,R3,T,T1,T2,T3,A,B,C)
381
           T10=T
382
           CALL INTERP(RM,R1,R2,R3,T,T4,T5,T6,A,B,C)
383
           T11=T
384
           DTR = (2*A*RM) + B
385
           CALL INTERP(RM, R1, R2, R3, T, T7, T8, T9, A, B, C)
386
           T12=T
387
           Z=LONI+ZI
           CALL INTERP(Z,Z1,Z2,Z3,T,T10,T11,T12,A,B,C)
388
389
           DTZ = (2*A*Z)+B
           TM=T
390
391
           IF(DTR.EO.0) THEN
392
                  ANGMJ=0.0D00
393
           ELSEIF(DTR.NE.O) THEN
394
                  ANGMJ=ASIN(1.0)
395
           ENDIF
```

```
IF(DTZ.GE.1.0E-30) ANGMJ=ATAN(DTR/DTZ)
396
           CALL INTERP(RM,R1,R2,R3,T,T4C,T5C,T6C,A,B,C)
397
           N1=N2
398
           N2=IOR+DT*((TM+T)/2)
399
400
           Al=SIN(ANGMJ-ANGIJ)
           A2=(N2/N1)*A1
401
           A3=ASIN(A2)
402
           ANGOJ=ANGMJ-A3
403
           ANGOJ=ANGMJ-ASIN((N2/N1)*SIN(ANGMJ-ANGIJ))
404 C
           RO=(ZI/2)*TAN(ANGOJ)+RM
405
           CALL REFINE(RO, ANGIJ, ANGMJ, ANGOJ, T4C, T5C, T6C)
406
407 C
           RETURN
408
           END
409
410 C
411 C
           SUBROUTINE FINAL (RO, ANGOJ)
412
413 C
           This subroutine calculates the final angle and radius out for
414 C
            all subsequent axial increments of the laser rod.
415 C
416 C
            REAL IOR, LONI, N1, N2
417
418 C
            DOUBLE PRECISION ANGMJ, ANGIJ, ANGOJ, A1, A2, A3, RI, RM, RO, Z, A, B, C
419
420 C
            COMMON /BLOCK1/IOR, DT, ACC, N1, N2, ZI, RI, RM, TM, LONI, I
421
            COMMON /BLOCK2/R1, R2, R3, Z1, Z2, Z3
422
            COMMON /BLOCK3/T1,T2,T3,T4,T5,T6,T7,T8,T9
423
            COMMON /BLOCK4/T1C, T2C, T3C, T4C, T5C, T6C, T10, T11, T12
424
425 C
426
            RI=RM
427
            RM=RO
428
            ANGIJ=ANGOJ
429
            IF(I.LT.10) CALL INTERP(RM,R1,R2,R3,T,T1C,T2C,T3C,A,B,C)
430
            IF(I.EQ.10) CALL INTERP(RM R1,R2,R3,T,T4C,T5C,T6C,A,B,C)
431
432
            DTR = (2*A*RM) + B
            CALL INTERP(RM,R1,R2,R3,T,T1,T2,T3,A,B,C)
 433
434
            T10=T
            CALL INTERP(RM, R1, R2, R3, T, T4, T5, T6, A, B, C)
 435
436
            T11=T
            CALL INTERP(RM, R1, R2, R3, T, T7, T8, T9, A, B, C)
 437
            T12=T
 438
            IF(I,LT.10) Z=LONI+ZI/2
 439
            IF(I.EQ.16) Z=LONI+ZI/2
 440
            CALL INTERP(Z, Z1, Z2, Z3, T, T10, T11, T12, A, B, C)
 441
 442
            DTZ = (2*A*Z) + B
            IF(DTR.EQ.O) THEN
 443
                    ANGMJ=0.0D00
 444
            ELSEIF(DTR.NE.0) THEN
 445
```

```
446
                    ANGMJ=ASIN(1.0)
 447
            ENDIF
 448
            IF(DTZ.GE.1.0E-30) ANGMJ=ATAN(DTR/DTZ)
 449
            TM=T
 450
            N1=N2
 451
            IF(I.LT.10) N2=IOR+DT*((TM+T11)/2)
 452
            IF(I.EQ.10) N2=IOR+DT*((TM+T12)/2)
 453
            Al=SIN(ANGMJ-ANGIJ)
 454
            A2 = (N2/N1) * A1
 455
            A3=ASIN(A2)
 456
            ANGOJ=ANGMJ-A3
 457 C
            ANGOJ=ANGMJ-ASIN((N2/N1)*SIN(ANGMJ-ANGIJ))
 458
            RO=(ZI/2)*TAN(ANGOJ)+RM
459
            IF(I.LT.10) CALL REFINE(RO, ANGIJ, ANGMJ, ANGOJ, T4, T5, T6)
 460
            IF(I.EQ.10) CALL REFINE(RO, ANGIJ, ANGMJ, ANGOJ, T7, T8, T9)
461 C
462
            RETURN
463
            END
464 C
465 C
466
            SUBROUTINE INTERP(R,R1,R2,R3,T,T1,T2,T3,A,B,C)
467 C
468 C
469 C
           The subroutine INTERP is a binomial interpolation routine using
            any three points in the R (radial) or Z (axial) direction to find
470 C
471 C
           the coefficients of A,B, and C of the equation AX**2 + BX + C = T
472 C
            so that a temperature T can be determined for any X (R or Z)
473 C
           within the non-linear temperature matrix.
474 C
475
           DOUBLE PRECISION R,A,B,C
476 C
477
           A=((T1-T2)*(R1-R3)-(T1-T3)*(R1-R2))/((R1-R3)*(R1**2-R2**2)-
478
          1 (R1-R2)*(R1**2-R3**2))
479
           B=((T1-T3)*(R1**2-R2**2)-(T1-T2)*(R1**2-R3**2))/((R1-R3)*
480
          1 (R1**2-R2**2)-(R1-R2)*(R1**2-R3**2)
481
           C=T1-A*R1**2-B*R1
           T=A*R**2+B*R+C
482
483 C
484
           RETURN
485
           END
486 C
487 C
488
           SUBROUTINE REFINE(RO, ANGIJ, ANGMJ, ANGOJ, T1, T2, T3)
489 C
490 C
491 C
           The subroutine REFINE is a continous numerical iteration routine
492 C
           used to recalculate the final thermal lensing output angle for
493 C
           each specified axial increment within each ray until the user
494 C
           specified accuracy criteria for the output angle are met.
495 C
```

```
496 C
    497
               REAL IOR, LONI, N1, N2
    498 C
    499
               DOUBLE PRECISION ANGMJ, ANGIJ, ANGOJ, Al, A2, A3, RI, RM, RO
    500
                DOUBLE PRECISION ROO, D, A, B, C
   501 C
   502
               COMMON /BLOCK1/IOR, DT, ACC, N1, N2, ZI, RI, RM, TM, LONI, I
   503
               COMMON /BLOCK2/R1, R2, R3, Z1, Z2, Z3
   504 C
   505
               L=0
             5 CONTINUE
   506
               L=L+1
   507
   508
               CALL INTERP(RO,R1,R2,R3,T,T1,T2,T3,A,B,C)
   509
               N2=IOR+DT*((TM+T)/2)
   510
               Al=SIN(ANGMJ-ANGIJ)
   511
               A2 = (N2/N1) * A1
   512
               A3=ASIN(A2)
   513
               ANGOJ=ANGMJ-A3
   514 C
               ANGOJ=ANGMJ-ASIN((N2/N1)*SIN(ANGMJ-ANGIJ))
               ROO=(Z1/2)*TAN(ANGOJ)+RM
   515
   516
               D=RO
               RO=ROO
   517
   518
               IF(ABS(D-ROO).GT.ACC) GOTO 5
   519 C
   520
               RETURN
   521
               END
No errors detected
```

Ĭ

Appendix B

Program Input Files

1. Thermal Lensing Model Input File #1

This file (THERLEN1.INP) contains thermal lensing material characteristics and other constants required to control the Thermal Lensing Model. The example data depicted below are for a pulsed side-pumped Nd:YAG rod.

Input File #1

THERMAL LENSING INPUT DATA FOR Nd:YAG ROD

```
1.15
37.5
; WAVELENGTH OF INTEREST (MICRONS)
37.5
; TEMPERATURE OF INTEREST (24-42 DEGREES C)
1.825
; INDEX OF REFRACTION
8.90E-06
; ALPHA (DN/DT)
0.33
; TEMPERATURE NORMALIZATION FACTOR
0.05
; TIME NORMALIZATION FACTOR
1
; O - RELATIVE VALUES IN INPUT FILE; 1 - ACTUAL VALUES
0.10
; AXIAL INCREMENT
1.0
; POWER MULTICATION FACTOR
1.0E-06
; OUTPUT ANGLE ACCURACY CRITERIA
0
; TYPE OF PUMPING (0=side, 1=end)
```

2. Thermal Lensing Model Input File #2

This file (THERLEN2.INP) is the output file from the model titled: Temperature Distribution Model for finite optically pumped laser rods. It contains that model's control criteria and output temperature data blocks versus time.

Those data blocks of temperatures contained within

this input file are used in the Thermal Lensing Model to calculate the thermal lensing and pump beam distortion effects. The example data depicted below are for a pulsed side-pumped Nd:YAG laser at its steady-state equilibrium temperature. Blocks of temperature data are shown from 3.4-3.6 seconds.

Input File #2

```
Input Nd:YAG Side-Pump..MP(20)..GA=20..GL=None..Run=001 03/01/90
                          MAX. AND INCREMENT OF RADIUS OF ROD -01 2.500000E-01
                                                                                                                   2.500000E-01
             MIN.
 2.500000E-01 2.500000E-01
....MIN, MAX AND INCR. OF ASPECT RATIO (L/A)
                                                                                                                            30.400000
.... MIN , MAX AND INCR. OF ASPECT RATIO (L/A)
30.400000 50.0000000
.... INVERSE OF RADIAL THERMAL DIFFUSIVITY 26
.... THERMAL CONDUCTIVITY 1.030000E-01 1.03000
.... MIN. RADIAL COOLING PARAMETER 20.000000
.... MAX. RADIAL COOLING PARAMETER 20.000000
TYPE OF SCALE 1(LOG) OR 0(LINEAR) 1
AND INCREMENT (SET TO 1. IF LOG) 1.000000
.... MIN. AND MAX. FRONT COOLING RATIO OR VALUES
6.500000E-04
                                                                                                                 26.947000
                                                                                                        1.030000E-01
                                                                                                                               6.500000E-04
6.500000E-04
TYPE OF SCALE 1(LOG) OR O(LINEAR)
AND INCREMENT (SET TO 1 IF LOG)
.....MIN. AND MAX. BACK COOLING RATIO OR VALUES
                                                                                                                               6.500000E-04
    6.500000E-04
TYPE OF SCALE 1(LOG) OR O(LINEAR)
AND INCREMENT (SET TO 1 IF LOG)
..... TYPE OF DATA RATIO=0 ACTUAL=1
                                                                                                    \bar{1}.000000
                                                  PARAM=2
 PROPORTIONAL TO L/A=3

VARIATION OF END DATA SEPERATE=0

TOGETHER=1
                                                                                                                   2
 MAXIMUM NUMBER OF ROOTS ... RADIAL MAXIMUM NUMBER OF ROOTS .. LONGIT NUMBER OF ORTHOGONAL CHECKS RADIA NUMBER OF ORTHOGONAL CHECKS LONGIT
                                                                                                                 17
                                                                                                                 17
                                                                                                                    23
                                                                               LONGIT
                                                                           COMPUTED
              BESSEL ROOTS SCHEME ...
                                                                           GIVEN
                                                                           ALL (GIVEN <21)
(COMPUTED GE 21)
```

```
ROOTS SCHEME IS
                  RADIAL AND LONG. INTEGRATION DIVISIONS
TYPE OF PUMP BEAM
RADIAL EIGENFUNCTION -OR
                                                                                                                                                                                                                                                                                1000
                                                                                                                                                                                                                                                                                                                                                       100
                                                                                                                                                                                                                   -ORDER
                                                                                          SQUARE PULSE
                                                                                                                                                                                                                   +0
                                                                                         GAUSSIAN
                                                                                                                                                                                                                  +1
                                                                                         PARABOLIC
                                 LONGIT
                                                                                         EIGNFUNCTION
                                                                                                                                                                                                                  -ORDER
                                                                                         CONSTANT
                                         CONSTANT +0
CONSTANT & ATTENUATED +1
FOCUSED(DEFOCUSED) +2
FOCUSED & ATTENUATED +3
NOTE NO DIFFRACTION EFFECTS ALLOWED
GAUSSIAN ENVELOPE ASSUMED
                                                                                                                                                                                                                +0
              PUMP BEAM CODE
            PUMP BEAM CODE

..... ATTENUATION DATA..O=ATTEN..1=ATTEN*L

.... OPTICAL DATA 3.000000

.... NUMBER OF RADIAL PROFILES ...

.... NUMBER OF LONGIT PROFILES ...

.... CONTINUOUS PUMPPING ... 0

.... SINGLE PULSE ... 1

OR MULTI-PULSED ... 2

MIN_REL_TIME_OF_INTERPST ... 3.400
SINGLE PULSE

OR MULTI-PULSED

MIN. REL. TIME OF INTEREST

MAX. REL. TIME OF INTEREST

MULTIPLE PULSES

MULTIPLE PULSES

MULTIPLE PULSES

MULTIPLE PULSE

MULT
                                                                                                                                                                                                                                                                                                                                              1.000000
                                                                                                                                                                                                                                                                                                                                                                      1.000000
                                                                                                                                                                                                                                   0.000000E+00
    ROD ASPECT RATIO (L/A) ..... =
                                                                                                                                                                                                                                          30.400000
    ******************************
    PARAMETER GA IS 20.000000 ***************
   PARAMETER GL OF FRONT
                                                                                                                                         6.500000E-04
  PARAMETER GL OF BACK 6.50000E-04 *************
```

	,	TEMPERATURE D									
		. DIFFUSIVITY		240470	NE+02						
		S OF ROD			0000						
		OF ROD		7.60							
		N SECONDS		345013							
	TIME .	in accomba									
L/R	.00	.10	.20	.30	.40	.50	.60	.70	.80	.90	1.00
.00	.72382E+00	.72383E+00	.72383E+00	.72383E+00		.72383E+00	.72383E+00		.72383E+00	.72383E+00	.72382E+00
.10	.71330E+00	.71331E+00	.71331E+00	.71331E+00	.71331E+00	.71331E+00	.71331E+00	.71331E+00	.71331E+00	.71331E+00	.71330E+00
.20	.69403E+00	.69404E+00		.69404E+00	.69404E+00	.69404E+00	.69404E+00	.69404E+00	.69404E+00	.69404E+00	.69403E+00
.30	.66320E+00	.66320E+00		.66320E+00	.66320E+00	.66320E+00	.66320E+00	.66320E+00	.66320E+00	.66320E+00	.66320€+00
.40	.62046E+00	.62046E+00	.62046E+00	.62046E+00	.62046E+00	.62047E+00	.62046E+00	.62046E+00	.62046E+00	.62046E+00	.62046E+00
.50	.56521E+00	.56522E+00	.56522E+00	.56522E+00		.56522E+00	.56522E+00	.56522E+00	.56522E+00	.56522E+00	.56521E+00
.60	.49688E+00	.49689E+00	.49689E+00	.49689E+00		.49689E+00	.49689E+00	.49689E+00	.49689E+00	.49689E+00	.49688E+00
.70	.41552E+00	.41552E+00	.41552E+00	.41552E+00		.41552E+00	.41552E+00	.41552E+00	.41552E+00	.41552E+00	.41552E+00
.80	.32288E+00	.32288E+00	.32288E+00	.32288E+00		.32288£+00	.32288E+00	.32288E+00	.32288E+00	.32288E+00	.32288E+00
.90	.22190E+00	.22190E+00	.22190E+00	.22190E+00	.22190E+00	.22190E+00	.22190E+00	.22190E+00	.22190E+00	.22190E+00	.22190E+00
1.00	.10556E+00	.10556E+00	.10556E+00	. 10556E+00	.10556E+00						
		TEMPERATURE C	ISTRIBUTION								
	RADIA	DIFFUSIVITY	·	269470	DE+02						
	RADIU	S OF ROO			0000						
	LENGTI	H OF ROD		7.60	00000						
	TIME	IN SECONDS		350000	DE+01						
L/R	.00	.10	.20	.30	.40	.50	.60	.70	.80	.90	1.00
.00	.64627E+00	.64627E+00		.64627E+00	.64627E+00	.64627E+00	.64627E+00	.64627E+00	.64627E+00	.64627E+00	.64627E+00
.10	.64006E+00	.64007E+00	.64007E+00	.64007E+00	.64007E+00	.64007E+00	.64007E+00	.64007E+00	.64007E+00	.64007E+00	.64006E+00
.20	621445+00	.62145E+00		.62145E+00		.62145E+00	.62145E→00	.62145E+00	.62145E+00	.62145E+00	.62144E+00
.30		,59041E+00		.59041E+00		.59041E+00	.59041E+00	.59041E+00	.59041E+00	.59041E+00	.59041E+00
.40		.54694E+00		.54694E+00		.54694E+00	.54694E+00	.54694E+00	.54694E+00	.54694E+00	.54693E+00
.50		.49096E+00		.49096E+0C	.49096E+00	.49096E+00	.49096E+00	.49096E+00	.49096E+00	.49096E+00	.49096€+00
.50	.42244E+00	.42244E+00	.42244E+00	.42244E+00	.42244E+00	.42244E+00	.42244E+00	.42244E+00	.42244E+00	.42244E+00	.42244E+00
.70		.34169E+00	.34169E+00	.34169E+00	.34169E+00	.34169E+00	.34169E+00	.34169E+00	.34169E+00	.34169E+00	.34169E+00
.80	.25008E+00	.25008E+00	.25008E+00	.25008E+00		.25008E+00	.25098£+00	.25008E+00	.25008E+00	.25008E+00	.25008£+00
.90		.15093E+00		.15093E+00		.15093E+00	.15093E+00	.15093E+00	.15093E+00	.15093E+00	.15093E+00
1,00	.49856E-01			.49857E-01		.49857E-01	.49857E-01	.49857E-01	.49856E-01	.49856E-01	.49856E-01
		TEMPERATURE (NULTIBLE ETST								
		L DIFFUSIVITY		269470	DE+02						
		S OF ROO			50000						
		H OF ROD			20000						
		TH SECONDS		350013							
L/R	.00	.10	.20	.30	.40	.50	.60	.70	.80	.90	1.00
.00	.72382E+00	.72383£+00	.72383E+00	.72383E+00	.72383E+00	.72383E+00	.72383E+00	.72383E+00	.72383E+00	.72383E+00	.72382E+00
.10	.71330E+00	.71331E+00	.71331E+00	.71331E+00	.71331E+00	.71331E+00	.71331E+00	.71331E+00	.71331E+00	.71331E+00	.713306+00
.20	.69403E+00	.69404E+00	.69404E+00	.69404E+00	.69404E+00	.69404E+00	.69404E+00	.69404E+00	.69404E+06	.69404E+00	.69403E+00
.30	.66320E+00	.66321E+00	.66321E+00	.66321E+00	.66321E+00	.66321E+00	.66321E+00	.66321E+00	.66321E+00	.66321E+00	.66320E+00
.40	.62046E+00	.62047E+00	.62047E+00	.62047E+00	.62047E+00	.62047E+00	.62047E+00	.62047E+00	.62047E+00	.62047E+60	.62046E+00
.50	.56521E+00	.565226+00	.56522E+00	.56522E+00	.56522E+00	.56522E+00	.56522E+00	.56522£+00	.56522E+00	,56522E+00	.56521E+00
.60	.496886+00	.49689E+00	.49689E+00	.49689E+00	.49689E+00	.49689E+00	.49689E+00	.49689E+00	.49689E+00	.49689E+00	.49688E+00
70	.41552F+00	.41552E+00	.41552E+00	-41552E+00	.41552E+00	.41552E+00	.41552E+00	.41552E+00	.41552E+00	.41552E+00	,41552E+0D

.70 .41552E+00 .41552E

	RAD I LENG	TEMPERATURE AL DIFFUSIVI US OF ROD TH OF ROD IN SECONDS		2694	250000 600000						
L/R .00 .10 .20 .30 .40 .50 .60 .70 .80	.00 .64627E+00 .64906E+00 .62144E+00 .59041E+00 .54694E+00 .42244E+00 .34169E+00 .25008E+00 .15093E+00	.10 .64627E+00 .64007E+00 .62145E+00 .59041E+00 .54694E+00 .42244E+00 .34169E+00 .25008E+00 .15093E+00	.20 .64627E+00 .64007E+00 .62145E+00 .59041E+00 .59041E+00 .49097E+00 .42244E+00 .34169E+00 .25008E+00 .15093E+00	.30 .64627E+00 .64007E+00 .62145E+00 .59041E+00 .59041E+00 .49097E+00 .42244E+00 .34169E+00 .25008E+00 .15093E+00	.40 .64628E+00 .64007E+00 .62145E+00 .59042E+00 .54694E+00 .49097E+00 .34169E+00 .25008E+00 .15093E+00	.50 .64628E+00 .64007E+00 .62145E+00 .59042E+00 .54694E+00 .49097E+00 .42244E+00 .34169E+00 .25008E+00 .15093E+00	.60 .64628E+00 .64007E+00 .62145E+00 .59042E+00 .54694E+00 .42244E+00 .34169E+00 .25008E+00 .15093E+00	.70 .64627E+00 .64007E+00 .62145E+00 .59041E+00 .54694E+00 .49097E+00 .42244E+00 .34169E+00 .25008E+00 .15093E+00	.80 .64627E+00 .64007E+00 .62145E+00 .59041E+00 .54694E+00 .49097E+00 .42244E+00 .34169E+00 .25008E+00 .15093E+00	.90 .64627E+00 .64007E+00 .62145E+00 .59041E+00 .54694E+00 .49097E+00 .42244E+00 .34169E+00 .25008E+00 .15093E+00	1.00 .64627E+00 .64006E+00 .62144E+00 .59041E+00 .49096E+00 .42244E+00 .34169E+00 .15093E+00 .49856E-01
	RAD I U LENGT	TEMPERATURE AL DIFFUSIVIT US OF ROO TH OF ROO IN SECONDS		26947	50000 00000						
L/R .00 .10 .20 .30 .40 .50 .60 .70 .89	.71331E+00 .69403E+00 .66320E+00 .62046E+00 .56521E+00 .4968BE+00 .32288E+00 .3228E+00 .10556E+00	.10 .72383E+00 .71331E+00 .69404E+00 .66321E+00 .62047E+00 .5652E+00 .49689E+00 .41552E+00 .32288E+00 .22190E+00 .10556E+00	.20 .72383E+00 .71331E+00 .69404E+00 .66321E+00 .66247E+00 .5652E+00 .49689E+00 .41552E+00 .32288E+00 .22190E+00 .10556E+00	.30 .72383E+00 .71331E+00 .69404E+00 .66321E+00 .5652E+00 .49689E+00 .41552E+00 .32288E+00 .22190E+00	.40 .72383E+00 .71331E+00 .69404E+00 .66321E+00 .5652E+00 .49689E+00 .41552E+00 .32288E+00 .22190E+00	.50 .72383E+00 .71331E+00 .69404E+00 .66321E+00 .5652E+00 .49689E+00 .41552E+00 .32288E+00 .22190E+00	.60 .72383E+00 .71331E+00 .69404E+00 .66321E+00 .56522E+00 .49689E+00 .32288E+00 .22190E+00 .10556E+00	.70 .72383E+00 .71331E+00 .69404E+00 .66321E+00 .56522E+00 .49689E+00 .3228BE+00 .22190E+00 .10556E+00	.80 .72383E+00 .71331E+00 .69404E+00 .66321E+00 .5652ZE+00 .49689E+00 .32288E+00 .32288E+00 .22190E+00	.90 .72383E+00 .71331E+00 .69404E+00 .66321E+00 .5652ZE+00 .49689E+00 .32288E+00 .32288E+00 .22190E+00	1,00 .72382E+00 .71331E+00 .69403E+00 .66320E+00 .62046E+00 .56521E+00 .49689E+00 .32288E+00 .22190E+00 .10556E+00
	RAD I U LENGT	L DIFFUSIVIT S OF ROO H OF ROO IN SECONDS		2	50000 00000						
.10 .20 .30 .40 .50 .60 .70	.00 .64613E+00 .63993E+00 .62131E+00 .59028E+00 .59028E+00 .49082E+00 .42230E+00 .34155E+00 .24995E+00 .15080E+00 .49752E-01	.10 .64613E+00 .63993E+00 .6213ZE+00 .5902BE+00 .54681E+00 .49083E+00 .42231E+00 .34156E#00 .24995E+00 .15080E+00 .49753E-01	.20 .64613E+00 .63994E+00 .6213ZE+00 .59028E+00 .59028E+00 .49083E+00 .42231E+00 .34156E+00 .24995E+00 .15080E+00 .49753E-01	.30 .64613E+00 .63994E+00 .62132E+00 .5902BE+00 .5902BE+00 .49085E+00 .42231E+00 .34156E+00 .24995E+00 .15080E+00 .49753E-01	.40 .64613E+00 .63994E+00 .62132E+00 .5902BE+00 .5902BE+00 .40083E+00 .42231E+00 .34156E+00 .24995E+00 .15080E+D0 .49753E-01	.50 .64613E+00 .63994E+00 .62132E+00 .5902B+00 .54681E+00 .49083E+00 .42231E+00 .34156E+00 .24995E+00 .15080E+00 .49753E-01	.60 .64613E+00 .63994E+00 .62132E+00 .5902BE+00 .49083E+00 .42231E+00 .34155E+00 .24995E+00 .15680E+00 .49753E-01	.70 .64613E+00 .63994E+00 .62132E+00 .59028E+00 .54681E+00 .42231E+00 .34156E+00 .24995E+00 .15080E+00	.49083E+00 .42231E+00 .34156E+00 .24995E+00 .15080E+00	.63994E+00 .62132E+00 .59028E+00 .54681E+00 .49083E+00 .42231E+00 .34156E+00 .24995E+00	1.00 .64613E+00 .63993E+00 .62131E+00 .59028E+00 .54680E+00 .42230E+00 .34155E+00 .24995E+00 .15080E+00 .49752E-01

Appendix C

Program Output File

Thermal Lensing Model Output File

The Thermal Lensing Model output file (THERLENS.OUT) rewrites the data from each of the input files. It then calculates thermal lensing and pump beam distortion effects for each block of temperature data obtained from the Temperature Distribution Model. Currently, the lensing model is programmed to calculate 10 equally spaced rays transiting through the laser material. The output data from the Thermal Lensing Model depicted below are for a pulsed sidepumped Nd:YAG laser using the input files in Appendix B.

Thermal Lensing Model Output File

THERMAL LENSING INFUT DATA FOR Nd:YAG ROD

.WAVELENGTH OF INTEREST IN UM..(WL): 1.150000

.....INPUT FILE #1.....

```
..WAVELENGTH OF INTEREST IN UM..(WL): 1.150000
..TEMPERATURE OF INTEREST IN DEG C..(TOI): 37.500000
.INDEX OF REFRACTION..(IOR): 1.825000
.ALPHA (dn/dt)..(DT): 8.900000E-06
..TEMP NORMALIZATION FACTOR..(TNF): 3.300000E-01
..TIME NORMALIZATION FACTOR..(TINF): 5.00000E-02
..O=RELATIVE TEMP; 1=ACTUAL TEMP..(IDATA): 1
.AXIAL INCREMENT FACTOR..(ZI): 1.000000E-01
..POWER MULTIPLICATION FACTOR..(FOWER): 1.000000
..OUTPUT ANGLE ACCURACY CRITERIA. (ACC): 1.000000E-06
..TYPE OF PUMPING (0=side, 1=end)..: 0.000000E+00
```

......INPUT FILE #2..... Input Nd: YAG Side-Pump..MP(20)..GA=20..GL=None..Run=001 03/01/90 MAX. AND INCREMENT OF RADIUS OF ROD 2.500000E-01 2.500000E-01 2.500000É-01 MIN , MAX AND INCR. OF ASPECT RATIO (L/A) 30.400000 50.000000 30.400000 30.400000 50.000000 INVERSE OF RADIAL THERMAL DIFFUSIVITY THERMAL CONDUCTIVITY 1.030000E-01 26.947000 1.030000E-01 THERMAL CONDUCTIVITY 1.030000E-01 1.03000 MIN. RADIAL COOLING PARAMETER 20.000000 MAX. RADIAL COOLING PARAMETER 20.000000 TYPE OF SCALE 1(LOG) OR 0(LINEAR) 1 AND INCREMENT (SET TO 1. IF LOG) 1.000000 MIN. AND MAX, FRONT COOLING RATIO OR VALUES 6.500000E-04 6.500000E-04 TYPE OF SCALE 1(LOG) OR O(LINEAR) 1 AND INCREMENT (SET TO 1 IF LOG) 1.000000MIN. AND MAX. BACK COOLING RATIO OR VALUES 6.500000E-04 6.500000E-04 TYPE OF SCALE 1(LOG) OR O(LINEAR) AND INCREMENT (SET TO 1 IF LOG) TYPE OF DATA RATIO=0 ACTUAL=1 1.000000 PARAM=2 PROPORTIONAL TO L/A=3..... VARIATION OF END DATA SEPERATE=0 2 17 17 RADIAL LONGIT BESSEL ROOTS SCHEME ... COMPUTED GIVEŅ ALL (GIVEN <21) (COMPUTED GE 21) ROOTS SCHEME IS RADIAL AND LONG. INTEGRATION DIVISIONS TYPE OF PUMP BEAM RADIAL EIGENFUNCTION -OR 1000 100 -ORDER SQUARE PULSE +() GÀUSSIAN +1 PARABOLIC

```
LONGIT
               EIGNFUNCTION
                                     -ORDER
      CONSTANT +0

CONSTANT & ATTENUATED +1

FOCUSED (DEFOCUSED) +2

FOCUSED & ATTENUATED +3

NOTE NO DIFFRACTION EFFECTS ALLOWED

GAUSSIAN ENVELOPE ASSUMED
  PUMP BEAM CODE
  PUMP BEAM CODE 0 0
..... ATTENUATION DATA..O=ATTEN..1=ATTEN*L
.....OPTICAL DATA 3.000000
.... NUMBER OF RADIAL PROFILES ...
                                                         1
                                                11
.... NUMBER OF LONGIT PROFILES ...
                                                              1.000000
                                                                  1.000000
                                          0.000000E+00
 ROD ASPECT RATIO (L/A) ..... =
                                            30.400000
```

TEMPERATURE DISTRIBUTION

RADIAL DIFFUSIVITY	26947CE+02
RADIUS OF ROO	250000E+00
LENGTH OF ROO	760000E+C1
TIME IN SECONDS	345000F+01

L/R	.00	_10	.20	.30	.40	.50	.60	.70	.80	.90	1.00
.00	.64626E+00	.64627E+00	.64626E+00								
.10	.64006E+00	.64006E+00	.64006E+00	.64005E+00	.64006E+00	.64006E+60	.64006E+00	.64006E+00	.64006E+G0	.64005E+00	.64006E+00
.20	.62144E+00	.62144E+00	.62144E+00	.62144E+00	.52144E+00	.62144E+00	.62144E+00	.62144E+00	.62144E-00	.62144E+00	.62144E+00
.30	_59040E+00	.59041E+00	.59041E+00	.59041E+00	.59041E+00	.59041E+00	.590/1E+00	.59041E+00	.59041E+00	.59041E+00	.59040E+00
.40	.54693E+00	.54694E+00	.54693E+00								
.50	.49096E+00										
.60	.42244E+00	.42244E+00	.42244E+00	.42244E+00	.42244E÷00	.42244E+00	.42244E+00	.42244E+00	.42244E+00	.42244E+00	.42244E+00
.70	.34169E+00	.34169£+00	.34169E+00	.341695+00	.34169E+00						
.80	.25008E+00	.250085+00	.25008E+00	.25008E+00	,25008E+00	.25008E+00	.25008E+00	.25008E+00	25008E+00	.25008E+00	.25008E+00
.90	.15093E+00										
1.00	.49853E-01	.49856E-01									

THERMAL LENSING PROGRAM OUTPUT DATA

INDEX OF REFRACTION MATRIX

.00	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01
.10	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	. 18250E+01	.18250E+01	.18250E+01	.18250E+01	. 18250E+01
.20	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	. 18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01
.30	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01
.40	.18250E+01	.18250E+01	.182506+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01
.50	.18250E+01	.18250£+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01
.60	,18250E+01	.18250£+01	.18250E+01	.182596+01	.18250E+01	.18250E+01	.18250E+01	. 18250E+01	.18250E+01	.18250E+01	.182506+01
.70	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	. 18250E+01
.80	. 18250E+01	.18250E+01	.18250E+01	.18250E+01	18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	. 18250E+01
.90	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250£+01	. 18250E+01
1.00	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250£+01	.1825GE+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01

THERMAL LENSING CALCUATIONS

 WAVELENGTH OF INTEREST(wn)
 .115000€+01

 TEMPERATURE OF INTEREST(deg C)
 .3750005+02

 TIME (sec)
 .345000€+01

RAY	ANGLE OUT	RADIUS	FOCAL	DISTORTION
(no.)	(radians)	(cm)	LENG(cm)	(X) ···
.00	.0000000£+G0	.0000000E+00	.000000CE+00	.0000000E+00
.10	.0000000E+00	.1000000E+00	CO+30000000.	.0000000E+00
.20	:00+30000000.	.20000000E+00	.6898527E+03	.000000000+00
.30	.0000000E+00	.3000000E+00	.7760843E+03	.1310063E-10
.40	.0090000E+00	.4000000E+00	.7884030E+C3	.1007527E-10
.50	.0000000E+00	.500000000;+00	.7839235E+03	.0000000E+00
.60	.0000000E+00	.6000000E+00	.7760843E+03	.0090000E+00
.70	.0000000E+0G	.7000000E+00	.7682449t+03	.00000000E+00
.80	.0000000E+00	.8000000E+00	.7612167E+03	.00/0000E+00
.90	.0000000E+0C	.9JJ00000E+00	.7551089E+03	.00000006+00
1.00	.0000000E+00	.0000000E+00	.0000C00E+00	.00G0000E+0G

.. END THERMAL LENSING OUTPUT..

.

TEMPERATURE DISTRIBUTION

RADIA! DIFFUSIVITY	269470E+02
RADIUS OF ROO	250000E+60
LENGTH OF ROD	760000E+01
TIME IN SECONDS	345013E+01

L/R .00	.00 .72382E+00	.10 .72383E+30	.20 .72383E+00	.30 .72383E+00	.40 .72383E+00	.50 .72383E+00	.60 .72383E+00	.70 .72383£+00	.80 .72383E+00	.90 .72383E+00	1.00 .72382E+00
.10	.71330E+00	.71331E+00	.71331E+00	.71331E+00	.71331£+00	.71331E+00	.71331E+00	.71331E+00	.71331E+00	.71331E+00	.71330E+00
.20	.69403E+00	.69404E+00	.69404E+00	.66320E+00	.694046+00	.69404E+00		.69404E+00	.69404E+90 .66320E+00	.59404E+00 .66320E+00	.69403E+00 .66320E+00
.40	.62046E+00	.62046E+00	.62046E+00	.62046E+00	.62046E+00			.62046E+00	.62046E+00	.62046E+00	.62046E+00
	.56521E+00	.56522£+00	.56522E+00	.56522E+00	.56522E+00	.55522E+00	.56522E+00 .49689E+00	.56522E+00 .49689E+00	.56522E+00 .49689E+00	.56522E+00 .49689E+00	.56521E+00 .49688E+00
.60 .70	.49688F+00 .41552E+00	.49689E+00	.49689E+00	.41552E+00	.49007E+00	.41552£+00	.41552E+00	.41552E+00	.41552E+00	.41552E+00	.41552E+00
.80	.32288E+00	.32288E+00	.32288E+00	.322886+00	.32288£+00	.32288E+00		.32288E+00	.32288E+00	.32288E+00	.32288E+00 .22190E+00
.90 1.00	.22190E+00 .10556E+00	.22190E+00 .10556E+00	.22190E+00 .10556E+00	.22190E+00 .10556E+00	.22190E+00 .10555E+00	.22190E+90 .10556E+00	.22190E+00 .10556E+00	.22190£+00 .10556£+00	.10556E+00	.10556E+00	.105566+00

THERMAL LENSING PROGRAM OUTPUT DATA

INDEX OF REFRACTION MATRIX

.00 .10 .20 .30 .40 .50 .60 .70	.18250E+01 18250E+01 18250E+01 18250E+01 18250E+01 18250E+01 18250E+01 18250E+01 18250E+01	.18250E+01 .18250E+01 .18250E+01 .18250E+01 .18250E+01 .18250E+01 .18250E+01 .18250E+01 .18250E+01 .18250E+01	.18250E+01 .18250E+01 .13250E+01 .18250E+01 .18250E+01 .18250E+01 .18250E+01 .18250E+01 .18250E+01	.18250E+01 .18250E+01 .18250E+01 .18250E+01 .18250E+01 .18250E+01 .18250E+01 .18250E+01 .18250E+01	.18250E+01 .18250E+01 .18250E+01	.18250E+01 .18250E+01 .18250E+01 .18250E+01 .18250E+01 .18250E+01 .18250E+01 .18250E+01 .18250E+01 .18250E+01	.18250E+01 .18250E+01 .18250E+01 .18250E+01 .18250E+01 .18250E+01 .18250E+01 .18250E+01 .18250E+01 .18250E+01	.18250E+01 .18250E+01 .18250E+01 .18250E+01 .18250E+01 .18250E+01 .18250E+01 .18250E+01 .18250E+01 .18250E+01 .18250E+01	.18250E+01 .18250E+01 .18250E+01 .18250E+01 .18250E+01 .18250E+01 .18250E+01 .18250E+01 .18250E+01 .18250E+01	.18250E+01 .18250E+01 .18250E+01 .18250E+01 .18250E+01 .18250E+01 .18250E+01 .18250E+01 .18250E+01 .18250E+01	.18250E+91 .18250E+01 .18250E+01 .18250E+01 .18250E+01 .18250E+01 .18250E+01 .18250E+01 .18250E+01 .18250E+01 .18250E+01
1.00	.18250E+01	.182506+01	.18250E+01	.18250E+01	.187508+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.162505+01

THERMAL LENSING CALCUATIONS

 WAVELENGTH OF INTEREST(Um)
 .115000E+01

 TEMPERATURE OF INTEREST(deg C)
 .375000E+02

 TIME (sec)
 .345013E+01

RAY	ARGLE OUT	RADIUS	FOCAL	DISTORTION
(no.)	(radians)	(cm)	LENG(cm)	(%)
.00	.000000002+00	.0000000E+00	.0000000E+00	.00430000000
.10	.00000000E+00	.1000000E+00	.3449263E+03	.5773156E-11
.20	.0000000E+00	.2000003E+00	.6898527E+03	.1398881E-10
.30	.000000002+00	50+3000000E.	.7760843E+03	.0000000E+00
.40	.0000000E+00	.4000000E+00	.6898527E+03	. 1333073E-08
.50	.0G000C0E+00	.50000000E+00	.7185965E+03	154765 i E-10
.60	.0000000E+00	.500000000+00	.7304323E+03	.2216745E+10
.70	.0000000E+00	.7000000E+06	.7348430E+03	.00000000E+00
.80	.0000000E+00	CO+2000COO8.	.7358428E+03	.00000000E+00
.90	.0000000E+00	.9060000E+00	.7551089E+03	00 00000E+ 03
1.00	.0000000000000	.0000000E+00	.000000002+00	.004306306+00

.. END THERMAL LENSING OUTPUT..

.....

TEMPERATURE DISTRIBUTION

RADIAL DIFFUSIVITY	′269470E+02
RADIUS OF ROD	250000E+00
LENGTH OF ROD	760000E+01
TIME IN SECONDS	350000E+01

L/R	.00	.10	.20	.30	.40	.50	.60	.70	.80	.90	1.00
.00	.64627E+00	.64627E+00	.64627£+00	.64627E+00							
. 10	.64006E+00	.64007E+00	.64006E+00								
. 20	.62144E+00	.62145E+00	.62145E+DO	.62145E+00	.62144E+DO						
.30	.59041E+60	.59041E+00	.59041£+00	.59041E+00	.59041E+00						
.40	.54693E+00	.54694E+00	.54694E+00	.54694E+00	,54694E+00	.54694E+00	.54694E+00	.54694E+00	.54694E+00	.54694E+00	.54693E+00
.50	.49096E+00										
.60	.42244E+00										
.70	.34169E+00										
.80	.25008E+00										
.90	.15093E+00										
1.00	.49856E-01	.49856E-01	.49856E-01	.49857E-01	.49857E-01	.49857E-01	.49857E-01	.49857E-01	.49856E-01	.49856E-01	.49856E-01

THERMAL LENSING PROGRAM OUTPUT DATA

INDEX OF REFRACTION MATRIX

.00	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01
.10	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01
.20	.18250E+01	.18250£+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01
.30	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01
.40	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01
.50	.18250E+01	.182506+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01
.60	. 18250£+01	.18250£+01	.18250£+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250€+01
.70	.18250E+01	.18250E+01	. 18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01
.80	.18250E+01	.18250£+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01
.90	.18250E+01	.182505+01	.18250E+01	.18250£+01	.18250E+01	.18250£+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01
1.00	.18250E+01	.18250E+01	.18250E+01	. 18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.182506+01	.18250E+01	.18250E+01

THERMAL LENSING CALCUATIONS

 WAVELENGTH OF INTEREST(um)
 .115000E+01

 TEMPERATURE OF INTEREST(deg C)
 .375000E+02

 TIME (sec)
 .350000E+01

RAY	ANGLE OUT	RADIUS	FOCAL	DISTORTION
(no.)	(radians)	(cm)	LENG(cm)	(%)
.00	.0000000E+00	.0000000E+00	.0000000E+00	.00000008+00
. 10	.00000000E+00	.1000000E+00	.0000000E+00	.4551913E-11
.20	.0000000E+00	.2000000E+00	.6898527E+03	1229572E-10
.30	.0000000E+00	.3020000E+00	.7760843E+03	.0000000E+00
.40	.00000000E+00	.4000000E+00	.7884030E+03	.9797715E-11
.50	.C000000E+00	.5000000E+00	.7839235£+03	.0000000E+00
.60	.0000000E+00	.6000000E+00	.7760843E+03	.0000000E+00
.70	.0000000E+00	.7000000E+00	.7682449E+03	.0000000E+00
.80	.0000000E+00	.8000000€+00	.7612167E+03	.00000000£+00
.90	.0000000E+00	,90000006+00	.7551089E+03	.00000000E+00
1.00	.0000000F+00	.0000000E+00	000000005+00	000000000+00

AVERAGE OF THE FOCAL LENGTHS (meters) = .677658E+01 INCREMENTAL DISTORTION (%) RANGES FROM 0.0 TO .980E-11

.. END THERMAL LENSING OUTPUT..

ORIGINAL PAGE IS OF POOR QUALITY

TEMPERATURE DISTRIBUTION

RADIAL DIFFUSIVITY	269470E+0Z
RADIUS OF ROO	250000£+00
LENGTH OF ROD	760000E+01
TIME IN SECONDS	350013E+01

L/R .00 .10 .20 .30 .40 .50 .60 .70	.00 .72382E+00 .71330E+00 .69403E+00 .66320E+00 .62046E+00 .56521E+00 .49688E+00 .32288E+00 .32288E+00	.10 .72383E+00 .71331E+00 .69404E+00 .66321E+00 .5652ZE+00 .49689E+00 .41552E+00 .32288E+00 .22190E+00	.20 .72383E^00 .71331E+00 .69404E+00 .66321E+00 .62647E+00 .56522E+00 .49689E+00 .41552E+00 .32288E+00 .22190E+00	.69404E+00 .66321E+00 .62047E+00 .56522E+00 .49689E+00 .41552E+00 .32288E+00 .22190E+00	.62047E+00 .56522E+00 .49689E+00 .41552E+00 .32288E+00 .22190E+00	.71331E+00 .69404E+00 .66321E+00 .62047E+00 .56522E+00 .49689E+00 .41552E+00 .32288E+00 .22190E+00	.62047E+00 .56522E+00 .49689E+00 .41552E+00 .32288E+00	.66321E+00 .62047E+00 .56522E+00 .49689E+00 .41552E+00 .32288E+00 .22190E+00	.56522E+00 .49689E+00 .41552E+00 .32288E+00 .22190E+00	.69404E+00 .66321E+00 .62047E+00 .56522E+00 .49689E+00 .41552E+00 .32288E+00 .22190E+00	1.00 .72382E+00 .71330E+00 .69403E+00 .66320E+00 .56521E+00 .49688E+00 .41552E+00 .32288E+00 .2190E+00
.90 1.00	.22190E+00 .10556E+00	.22190E+00 .10556E+00	.22190E+00 .10556E+00	.22190E+00 .10556E+00	.22190E+00 .10556E+00			.22190E+00 .10556E+00	.22190E+00 .10556E+00		

THERMAL LENSING PROGRAM OUTPUT DATA

INDEX OF REFRACTION MATRIX

	.18250E+01	. 18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	. 18250E+01	. 18250E+01	.18250E+01	.18250E+01	. 18250E+01
.00	.,			.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01
.10	.18250E+G1	.18250E+01	.18250E+01			.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	. 18250E+01
.20	.18250E+01	.18250E+01	.18250E+01	.18250E+01				. ,	.18250E+01	.18250E+01	.18250E+01
.30	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250£+01	.18250E+01	.18250E+01			
.40	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01
.50	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250£+01
		.1825CE+01	. 18250E+01	.18250E+01	.18250E+01	.18250£+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01
.60	.18250E+01			.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250€+01	.18250E+01
.70	.18250E+01	.18250E+01	.18250E+01		•		.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01
.80	.18250E+01	.18250E+01	.18250E+01	.18250E+01	. 18250E+01	.18250E+01		•	.18250E+01	.18250E+01	.18250E+01
.90	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+D1	.18250E+01	.18250E+01			
1 00	. 18250E+01	.18250E+01	.18250E+01	.1825CE+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01

THERMAL LENSING CALCUATIONS

 WAVELENGTH OF INTEREST(um)
 .115000E+01

 TEMPERATURE OF INTEREST(deg C)
 .375000E+02

 TIME (sec)
 .350013E+01

RAY	ANGLE OUT	RADIUS	FOCAL	DISTORTION
(no.)	(radians)	(cm)	LENG(cm)	(%)
.00	.00000002+00	.0000000E+00	.000000000000	.0000000E+00
.10	.00000000E+00	.1000000E+00	.3449263E+03	.5773156E-11
.20	.0000000E+00	.2000000E+0J	.6898527E+03	4718448Ē-11
.30	.0000000E+00	.3000000E+00	.7760843E+03	.3552712E-11
.40	.0000000E+00	.4000000E+00	.6898527E+03	.9936493E-11
.50	.00000000E+00	.5000000E+00	.7185965E+03	6661338E-12
.60	.0000000E+00	.60000000E+00	.7304323E+03	.2216745E-10
.70	.00000000E+00	.7000000£+00	.7348430E+03	.0007000E+00
.80	.0000000E+00	.8000000E+00	.7358428E+03	.00000000E+00
.90	.0000000E+00	.9000008+00	.7551089E+03	.0000000£+00
1 00	0000000E+00	.0000000E+G0	.0000000E+00	.00000000E+00

AVERAGE OF THE FOCAL LENGTHS (meters) = .686171E+01 INCREMENTAL DISTORTION (%) RANGES FROM 0.0 TO .222E-10

.. END THERMAL LENSING OUTPUT...

TEMPERATURE DISTRIBUTION

RADIAL DIFFUSIVITY	269470E+02
RADIUS OF ROO	250000E+00
LENGTH OF ROO	760000E+01
TIME IN SECONDS	355000E+01

L/R	.00	.10	.20	.30	.40	.50	.60	.70	.80	.90	1.00
.00	.64627E+00	.64627E+00	.64627E+00	.64627E+00	.64628E+00	.64628E+00	.64628E+00	.64627E+00	.64627E+00	.64627E+00	.64627F+00
. 10	.64006E+00	.64007E+00	.64007E+00	.64007E+00	.64007E+00	.64007E+00	.64007E+00	.64007E+00	.64007E+00	.64007E+00	.64006E+00
.20	.62144E+00	.62145E+00	.62145E+00	.62145E+00	.62145E+00	.62145E+00	.62145E+00	.62145E+00	.62145E+00	.62145E+00	.62144E+00
.30	.59041E+00	.59041E+00	.59041E+00	.59041E+00	.59042E+00	.59042E+00	.59042E+00	.59041E+00	.59041E+00	.59041E+00	.59041E+00
.40	.54694E+00	.54694E+00	.54694E+00	.54694E+00	.54694E+00	.54694E+00	.54694E+00	.54694E+00	.54694E+00	.54694E+00	.54694E+00
.50	.49096E+00	.49097E+00	.49097E+00	.49097E+00	.49097E+00	.49097E+00	.49097E+00	.49097E+00	.49097E+00	.49097E+00	.49096E+00
.60	.42244E+00	.42244E+00	.42244E+00	.42244E+00	.42244E+00	.42244E+00	.42244E+00	.42244E+00	.42244E+00	.42244E+00	.42244E+00
.70	.34169E+00	.34169E+00	.34169E+00	.34169E+00	.34169E+00	.34169E+00	.34169E+00	.34169E+00	.34169E+00	.34169E+00	.34169E+00
.80	.25008E+00	.25008E+00	.25008E+00	.25008£+00	.25008E+00						
.90	.15 0 93E+00	.15093E+00	. 15093E+00	. 150936+00	.15093E+00						
1.00	.49856E-01	.498575-01	.49857E-01	.49857E-01	.49857E-01	.49857E-D1	.49857F-01	.49857F-01	49857F-01	40857E-01	40854E-01

THERMAL LENSING PROGRAM OUTPUT DATA

INDEX OF REFRACTION MATRIX

.00	.18250E+01	.18250E+01	.18250E+01	.18250£+01	.18250£+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01
. 10	.18250E+01	-18250E+01	.18250E+01	. 18250E+01	.18250E+01						
.20	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.182506+01	.18250E+01	.18250E+01	.18250E+01
.30	.18250E+01	.18250E+01	.18250€+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01
.40	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250€+01	.18250E+01	.18250E+01	.18250E+01
.50	.18250£+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01
.60	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250£+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01
.70	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+C1	.18250E+01	.18250E+01
.80	.18250£+01	.18250£+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01
.90	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250£+01	.18250E+01
1.00	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01

THERMAL LENSING CALCUATIONS

RAY	ANGLE OUT	RADIUS	FOCAL	DISTORTION
(no.)	(radians)	(cm)	LENG(cm)	(%)
.00	.00000000E+00	.00000002+00	.0000000E+00	.DOCOOOOE+00
.10	.0000000E+00	.1000000E+00	.0000000E+00	.4551913E-11
.20	.0000000E+30	.2000000E+00	.6898527E+03	1229572E-10
.30	.0000000E+00	.3000000E+00	.7760843E+03	.9963511E-09
.40	.0000000E+00	.4000000E+00	.7884030E+03	.0000000E+00
.50	.00000000E+00	.5000000E+00	.7839235E+03	1709743E-11
.60	.00000000E+00	.6000000E+00	.7760843E+03	.00000000£+00
.70	.0000000E+00	.7000000E+00	.7682449E+03	.0000000E+00
.80	.000000000+00	.8000000E+00	.7612167E+03	.0000000E+00
. 90	.000000000000	.9000000E+00	.7551089E+03	.00000000E+00
1.00	.0000000E+00	.000000000+00	.0000000E+00	.00+30000000.

AVERAGE OF THE FOCAL LENGTHS (meters) = .677658E+01 INCREMENTAL DISTORTION (%) RANGES FROM 0.0 TO .996E-09

.. END THERMAL LENSING OUIPUT..

C-2

TEMPERATURE DISTRIBUTION

RADIAL	DIFFUSIVITY	269470E+02
RADIUS	OF ROC	250000E+09
LENGTH	OF ROO	760000E+01
TIME IN	SECONDS	355013E+01

L/R	.00	.10	.20	.30	.40	.50	.60	.70	.80	.90	1.00
.00	.72382£+00	.72383E+00	.72382E+00								
.10	.71331E+00										
.20	.69403E+00	.69404E+00	.69403E+00								
.30	.66320E+00	.66321E+00	.66320E+00								
.40	.62046E+00	62047E+00	.62047E+00	.62046E+00							
.50	.56521E+00	.56522E+00	.56521E+00								
.60	.49688E+00	.49689E+00	.496898+00	.49689E+00	.49689E+00						
.70	.41552E+00										
.80	.32288E+00	.32288€+00	.32288E+00	.32288E+00							
.90	.22190E+00										
1 00	10556E+00	10556E+00	10556E+00	10556E+00	105566+00	10556E+00	105566+00	10556E+00	10555E+00	10556E+00	105566+00

THERMAL LENSING PROGRAM OUTPUT DATA

INDEX OF REFRACTION MATRIX

.00	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01
.10	.18250E+01	.18250£+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250£+01	.18250E+01	.18250E+01	.18250E+01
.20	.182506+01	.18250£+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.182508+01	.18250E+01
.30	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	. 18250E+01	.18250E+01	.18250E+01	.18250E+01	.182506+01	.18250£+01
.40	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	. 18250E+01
.50	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	. 18250E+01	.18250E+01	. 18250E+01
.60	.18250E+61	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.182508+01	.18250E+01
.70	.18250£+01	.18Z50E+01	.182502+01	.1825GE+01	.18250E+01	.18250£+01	.18250£+01	.18250E+01	. 18250E+01	. 1825GE+01	.15250E+01
.80	.18250E+01	.18250£+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.182505+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01
.90	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.1825CE+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	.18250E+01	. 18250E+91
1.00	.18250E+01	.182502+01	. 18250E+01	.18250E+01	.18250E+01	.18250F+01	.18250E+01	. 18250F+01	.18250£+01	.18250F+01	.18250£+01

THERMAL LENSING CALCUATIONS

 WAVELENGTH OF INTEREST(um)
 .1150006+01

 TEMPERATURE OF INTEREST(deg C)
 .3750006+02

 TIME (sec)
 .355013E+01

RAY	ANGLE OUT	RADIUS	FOCAL	DISTORTION
(no.)	(radians)	(cm)	LENG(cm)	(%)
	••••••		*******	
.00	.0000000E+00	.0000000E+00	.00000006+00	.0000000E+00
. 10	.00000000E+00	.10000005+00	.3449263E+03	.00000000E+00
.20	.00000005+00	.2000000E+00	.6898527E+03	.2553516E-11
.30	.00000000E+00	.30000005+00	.7760843£+03	.3552712E-11
.40	.0000000E+00	.4000000F+00	.6898527E+03	.9936493E-11
.50	.0000000E+00	.5000000E+00	.7185965E+03	6661338E-12
.60	.0000000E+00	.6000000E+00	.7304323E+03	.2216745E-10
.70	.0000000E+00	.7000000E+00	.7348430E+03	.0000000E+00
.80	.0000000E+00	.8000000E+0C	.7358428E+C3	.0000000E+00
.90	.0000000E+00	.9000000E+00	.7551089E+03	.0000000E+00
1.00	.000000000+000	.0000000E+00	.0000000E+00	.0000000000+00

AVERAGE OF THE FOCAL LENGTHS (meters) = .886171E+01 INCREMENTAL DISTORTION (%) RANGES FROM 0.0 TO .222E-10

.. END THERMAL LENSING OUTPUT..

TO THE PROPERTY OF THE PARTY OF

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